

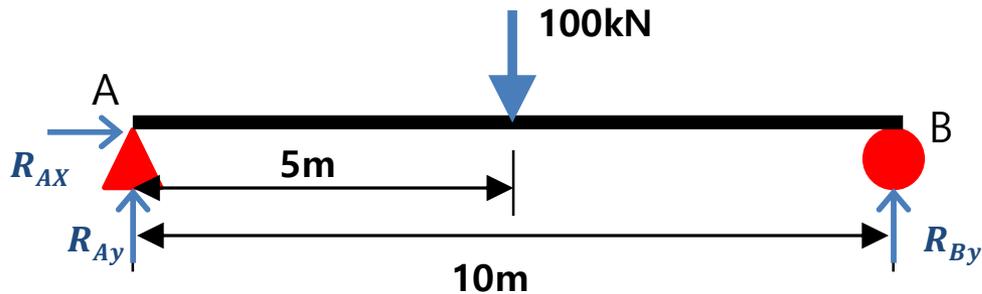
# 구조역학기초 2

부천대학교 토목공학과 박영훈 교수

# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

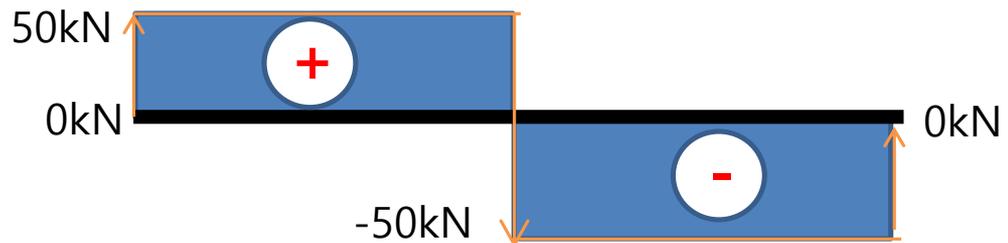
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 1)



$$M_A + \curvearrowright = 0, \quad (100\text{kN} \times 5\text{m}) - (R_{By} \times 10\text{m}) = 0, \quad R_{By} = 50\text{kN}$$

$$\uparrow F_y = 0, \quad R_{Ay} + R_{By} = 100\text{kN}, \quad R_{Ay} = 50\text{kN}$$

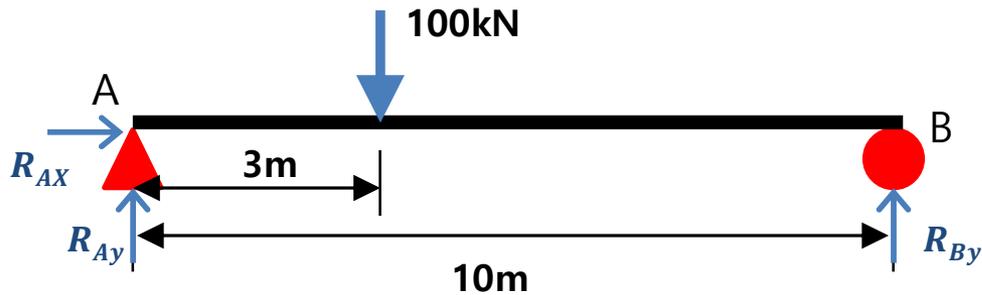
$$\rightarrow F_x = 0, \quad R_{Ax} = 0$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

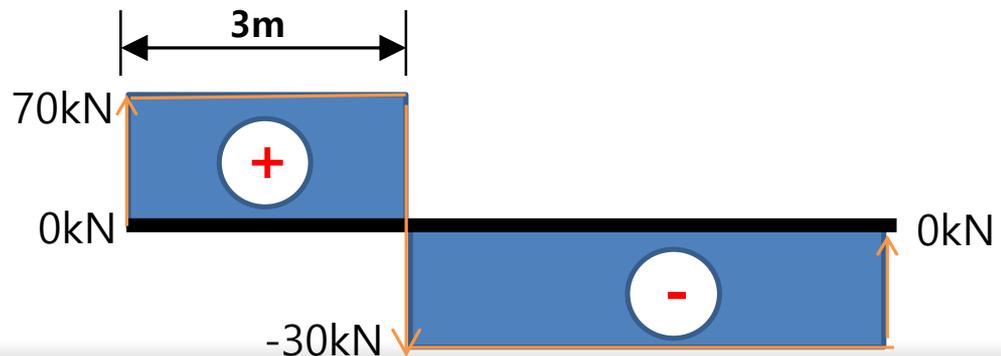
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 2)



$$M_A + \curvearrowright = 0, \quad (100\text{kN} \times 3\text{m}) - (R_{By} \times 10\text{m}) = 0, \quad R_{By} = 30\text{kN}$$

$$\uparrow F_y = 0, \quad R_{Ay} + R_{By} = 100\text{kN}, \quad R_{Ay} = 70\text{kN}$$

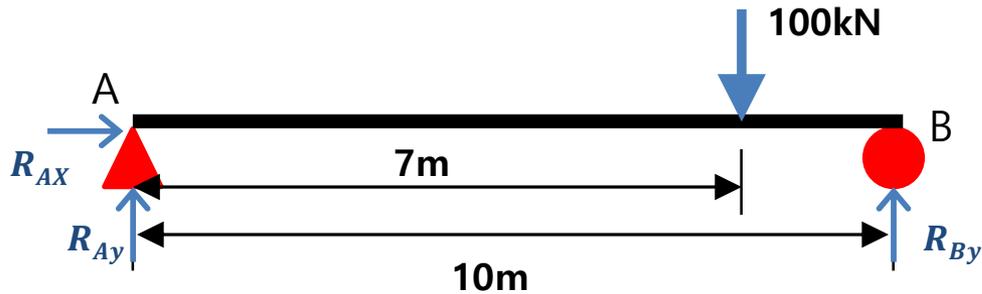
$$\rightarrow F_x = 0, \quad R_{Ax} = 0$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

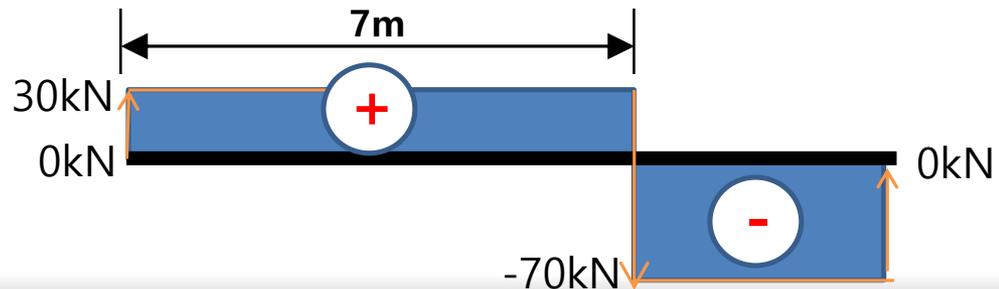
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 3)



$$M_A + \curvearrowright = 0, \quad (100\text{kN} \times 7\text{m}) - (R_{By} \times 10\text{m}) = 0, \quad R_{By} = 70\text{kN}$$

$$\uparrow F_y = 0, \quad R_{Ay} + R_{By} = 100\text{kN}, \quad R_{Ay} = 30\text{kN}$$

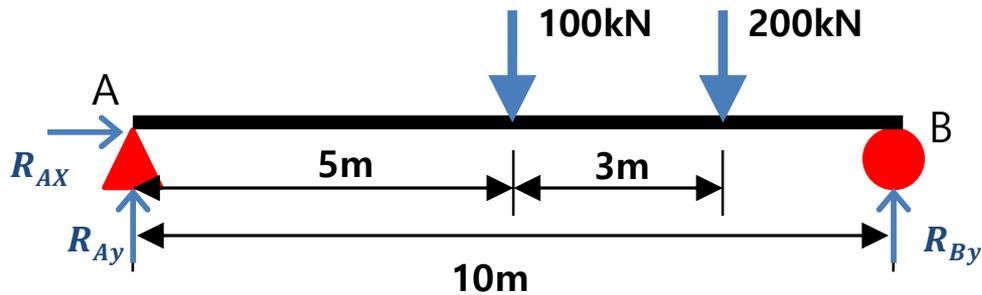
$$\rightarrow F_x = 0, \quad R_{Ax} = 0$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

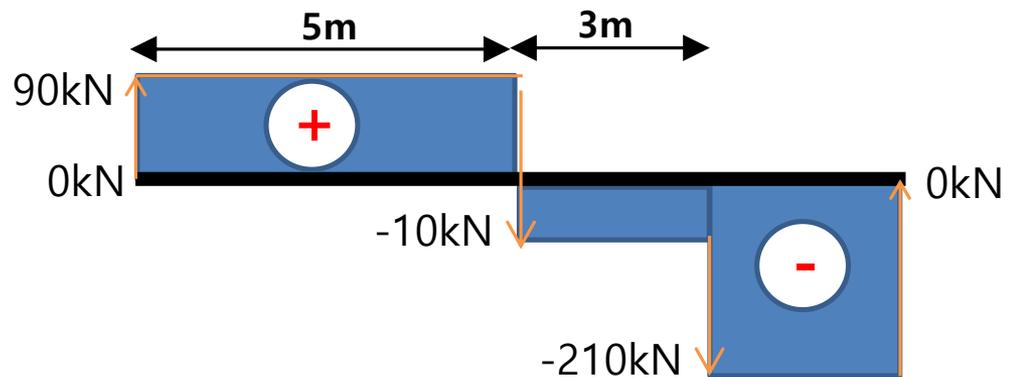
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 4)



$$M_A + \curvearrowright = 0, \quad (100\text{kN} \times 5\text{m}) + (200\text{kN} \times 8\text{m}) - (R_{By} \times 10\text{m}) = 0, \quad R_{By} = 210\text{kN}$$

$$\uparrow F_y = 0, \quad R_{Ay} + R_{By} = 300\text{kN}, \quad R_{Ay} = 90\text{kN}$$

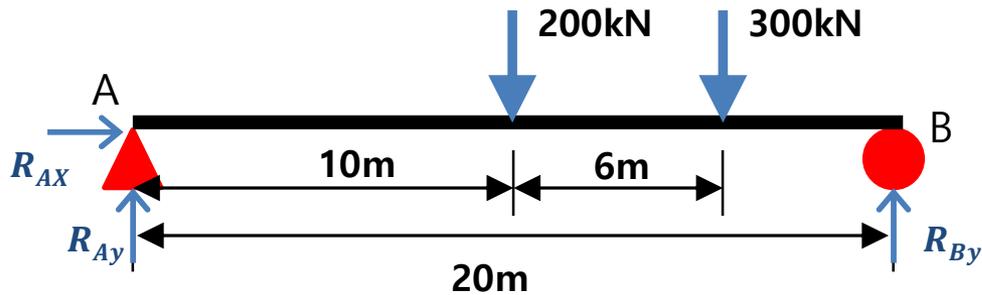
$$\rightarrow F_x = 0, \quad R_{Ax} = 0$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

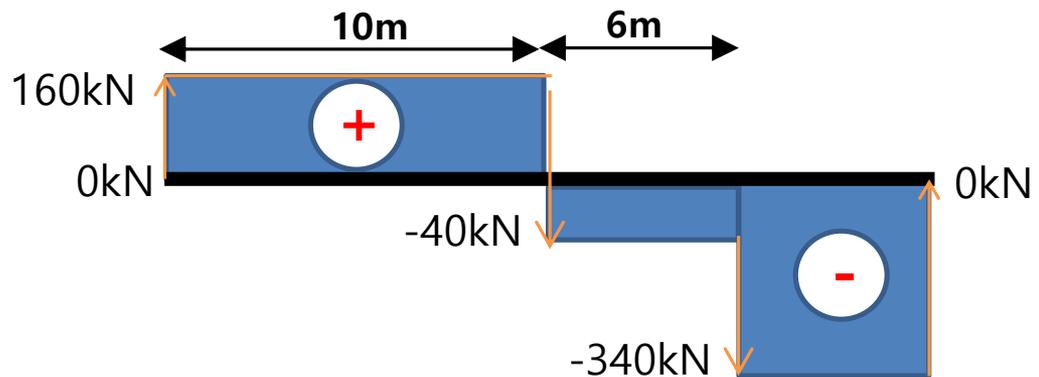
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 5)



$$M_A + \curvearrowright = 0, \quad (200\text{kN} \times 10\text{m}) + (300\text{kN} \times 16\text{m}) - (R_{By} \times 20\text{m}) = 0, \quad R_{By} = 340\text{kN}$$

$$\uparrow F_y = 0, \quad R_{Ay} + R_{By} = 500\text{kN}, \quad R_{Ay} = 160\text{kN}$$

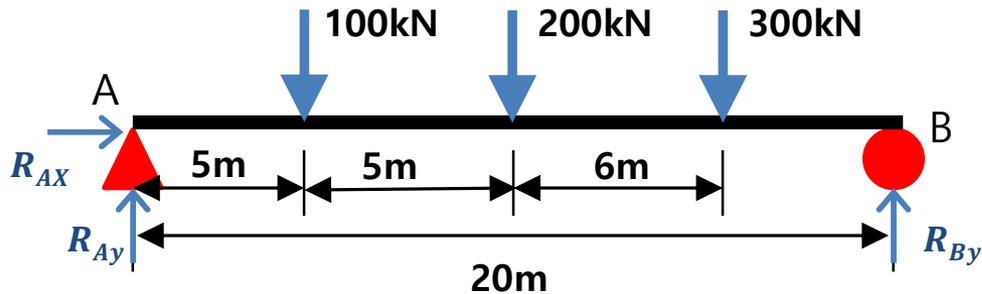
$$\rightarrow F_x = 0, \quad R_{Ax} = 0$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

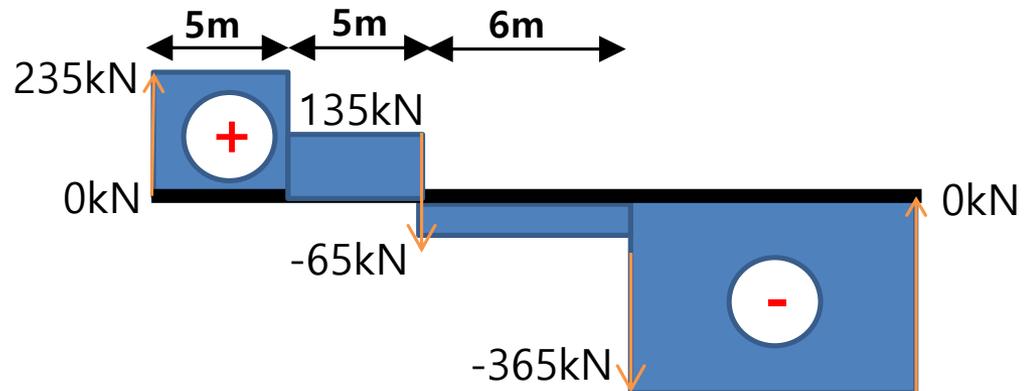
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 6)



$$M_A + \curvearrowright = 0, (100\text{kN} \times 5\text{m}) + (200\text{kN} \times 10\text{m}) + (300\text{kN} \times 16\text{m}) - (R_{By} \times 20\text{m}) = 0, R_{By} = 365\text{kN}$$

$$\uparrow F_y = 0, R_{Ay} + R_{By} = 600\text{kN}, R_{Ay} = 235\text{kN}$$

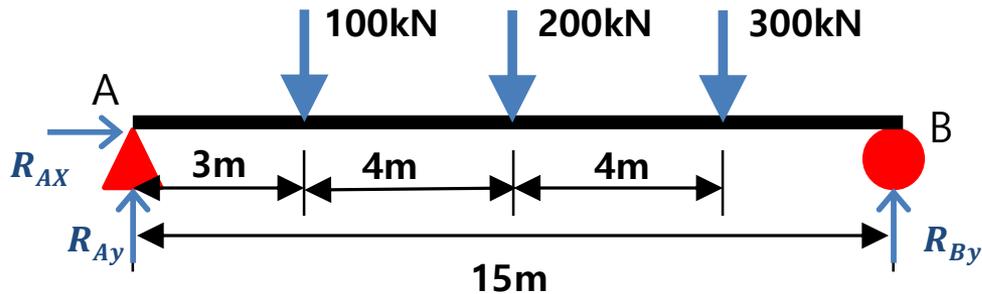
$$\rightarrow F_x = 0, R_{Ax} = 0$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

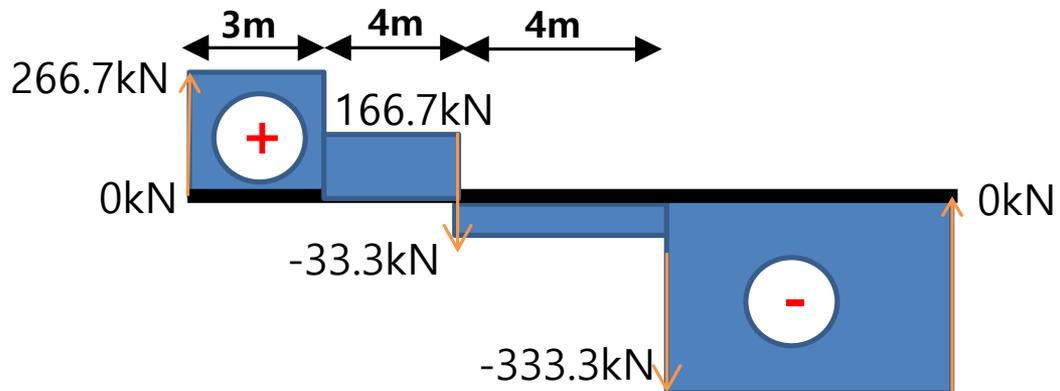
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 7)



$$M_A + \curvearrowright = 0, (100\text{kN} \times 3\text{m}) + (200\text{kN} \times 7\text{m}) + (300\text{kN} \times 11\text{m}) - (R_{By} \times 15\text{m}) = 0, R_{By} = 333.3\text{kN}$$

$$\uparrow F_y = 0, R_{Ay} + R_{By} = 600\text{kN}, R_{Ay} = 266.7\text{kN}$$

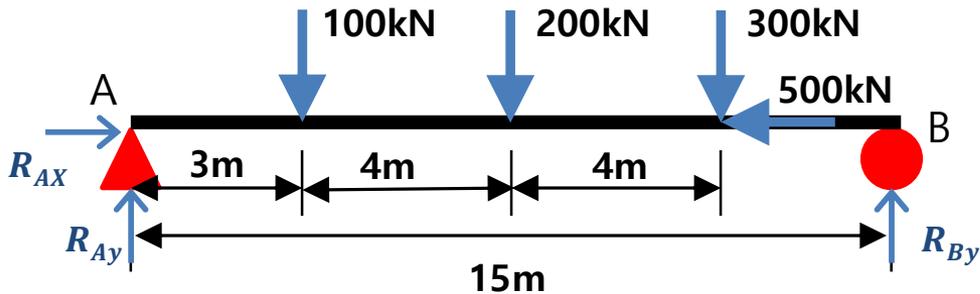
$$\rightarrow F_x = 0, R_{Ax} = 0$$



# VI. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

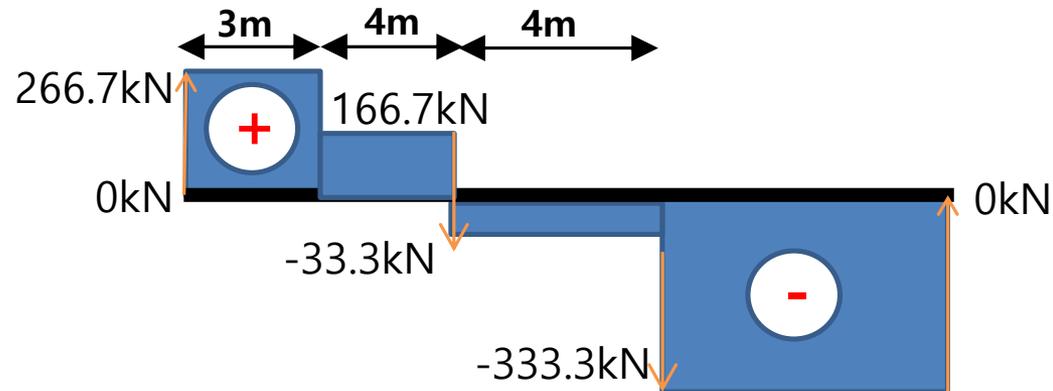
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 8)



$$M_A + \curvearrowright = 0, (100\text{kN} \times 3\text{m}) + (200\text{kN} \times 7\text{m}) + (300\text{kN} \times 11\text{m}) - (R_{By} \times 15\text{m}) = 0, R_{By} = 333.3\text{kN}$$

$$\uparrow F_y = 0, R_{Ay} + R_{By} = 600\text{kN}, R_{Ay} = 266.7\text{kN}$$

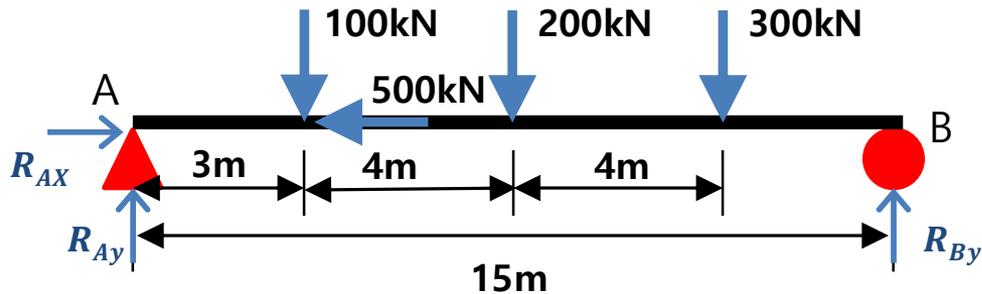
$$\rightarrow F_x = 0, R_{Ax} - 500\text{kN} = 0, R_{Ax} = 500\text{kN}$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

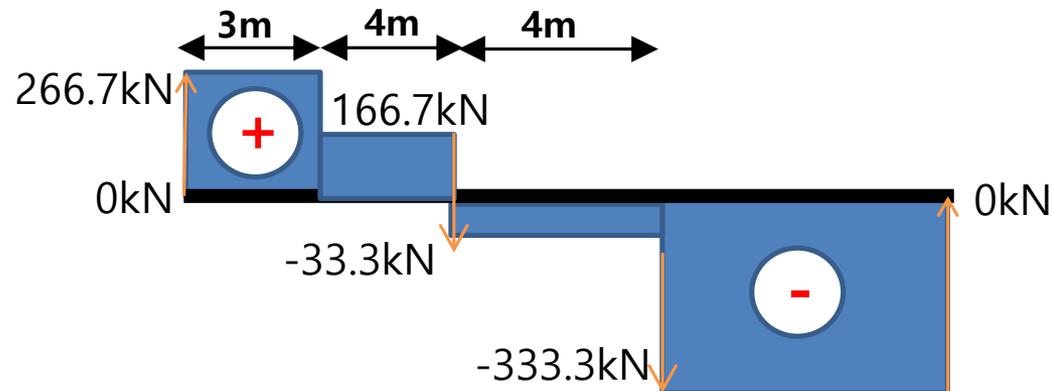
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 9)



$$M_A + \curvearrowright = 0, (100\text{kN} \times 3\text{m}) + (200\text{kN} \times 7\text{m}) + (300\text{kN} \times 11\text{m}) - (R_{By} \times 15\text{m}) = 0, R_{By} = 333.3\text{kN}$$

$$\uparrow F_y = 0, R_{Ay} + R_{By} = 600\text{kN}, R_{Ay} = 266.7\text{kN}$$

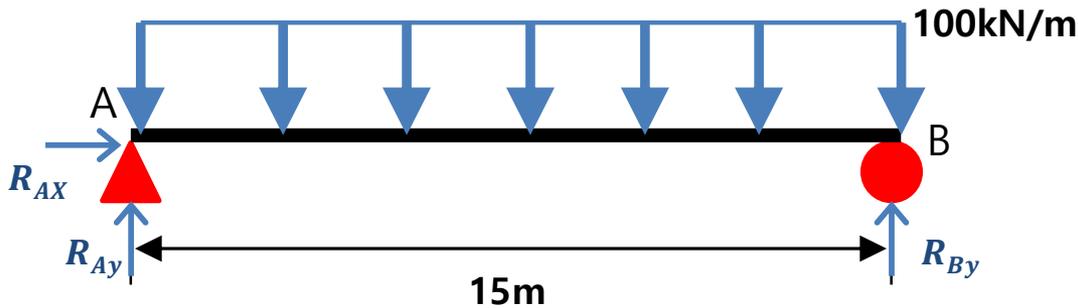
$$\rightarrow F_x = 0, R_{Ax} - 500\text{kN} = 0, R_{Ax} = 500\text{kN}$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

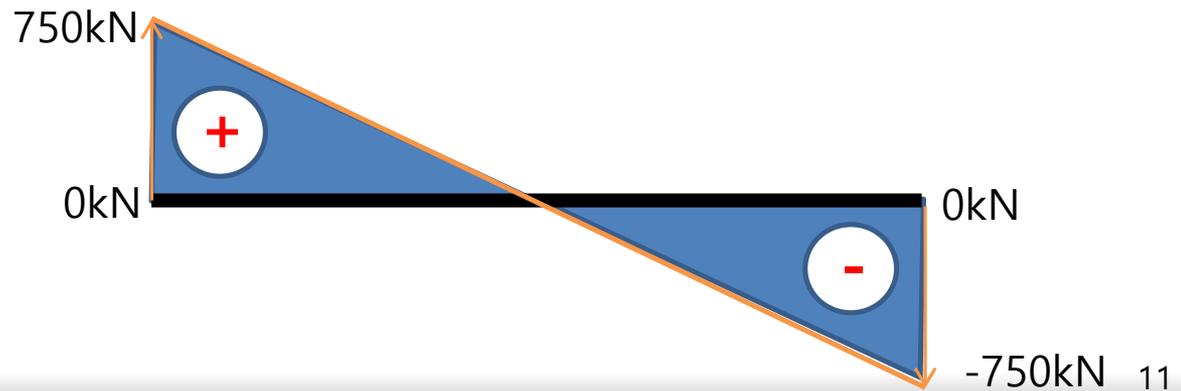
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 10)



$$M_A + \curvearrowright = 0, (100\text{kN} \times 15\text{m} \times 7.5\text{m}) - (R_{By} \times 15\text{m}) = 0, R_{By} = 750\text{kN}$$

$$\uparrow F_y = 0, R_{Ay} + R_{By} = 1,500\text{kN}, R_{Ay} = 750\text{kN}$$

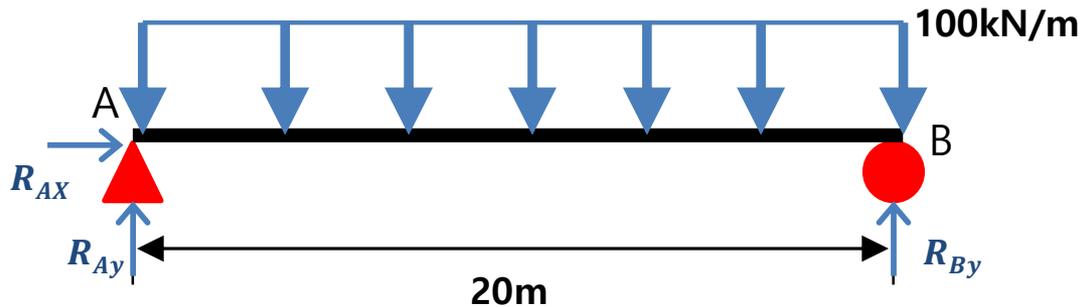
$$\rightarrow F_x = 0, R_{Ax} = 0$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

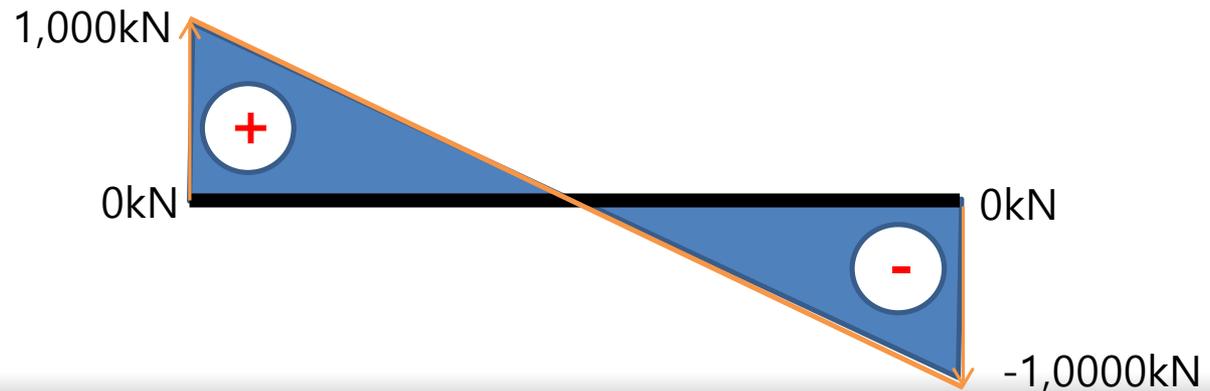
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 11)



$$M_A + \curvearrowright = 0, (100\text{kN} \times 20\text{m} \times 10\text{m}) - (R_{By} \times 20\text{m}) = 0, R_{By} = 1,000\text{kN}$$

$$\uparrow F_y = 0, R_{Ay} + R_{By} = 2,000\text{kN}, R_{Ay} = 1,000\text{kN}$$

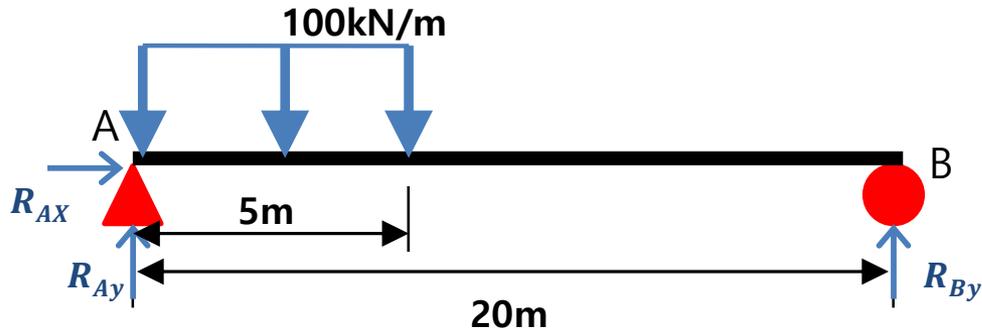
$$\rightarrow F_x = 0, R_{Ax} = 0$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

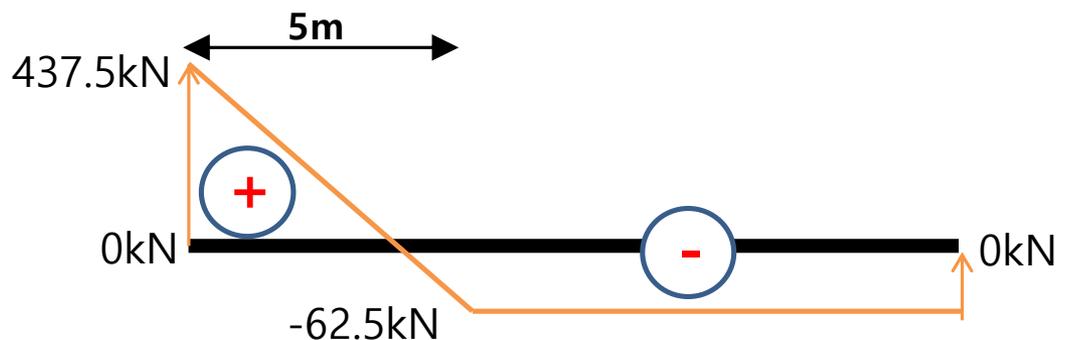
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 12)



$$M_A + \curvearrowright = 0, (100\text{kN} \times 5\text{m} \times 2.5\text{m}) - (R_{By} \times 20\text{m}) = 0, R_{By} = 62.5\text{kN}$$

$$\uparrow F_y = 0, R_{Ay} + R_{By} = 500\text{kN}, R_{Ay} = 437.5\text{kN}$$

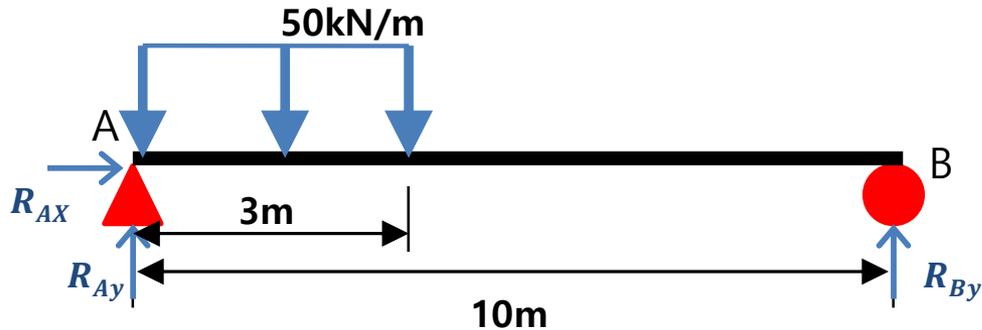
$$\rightarrow F_x = 0, R_{Ax} = 0$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

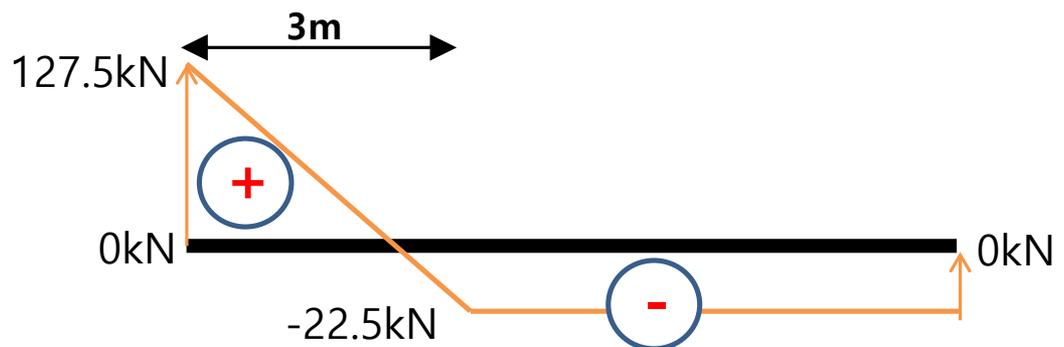
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 13)



$$M_A + \curvearrowright = 0, (50\text{kN} \times 3\text{m} \times 1.5\text{m}) - (R_{By} \times 10\text{m}) = 0, R_{By} = 22.5\text{kN}$$

$$\uparrow F_y = 0, R_{Ay} + R_{By} = 150\text{kN}, R_{Ay} = 127.5\text{kN}$$

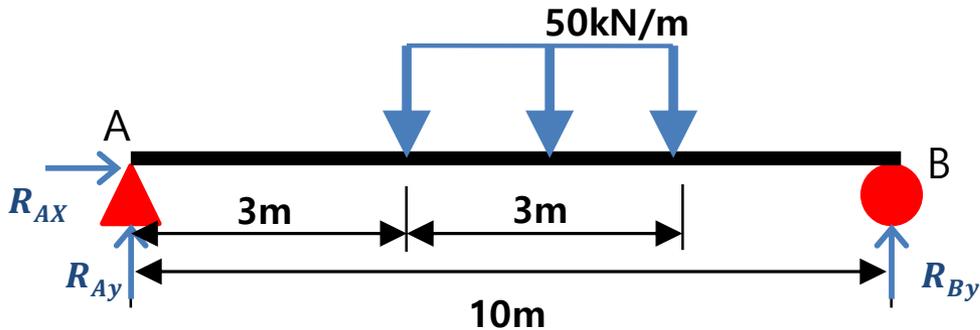
$$\rightarrow F_x = 0, R_{Ax} = 0$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

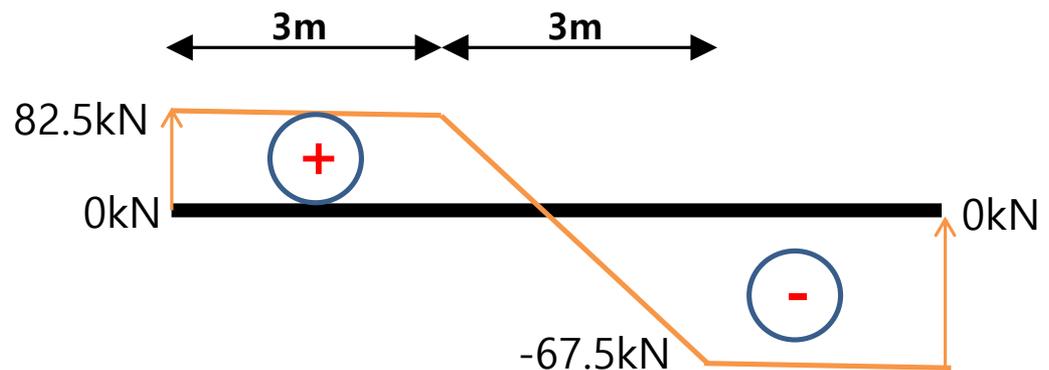
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 14)



$$M_A + \curvearrowright = 0, (50\text{kN} \times 3\text{m} \times (3+1.5)\text{m}) - (R_{By} \times 10\text{m}) = 0, R_{By} = 67.5\text{kN}$$

$$\uparrow F_y = 0, R_{Ay} + R_{By} = 150\text{kN}, R_{Ay} = 82.5\text{kN}$$

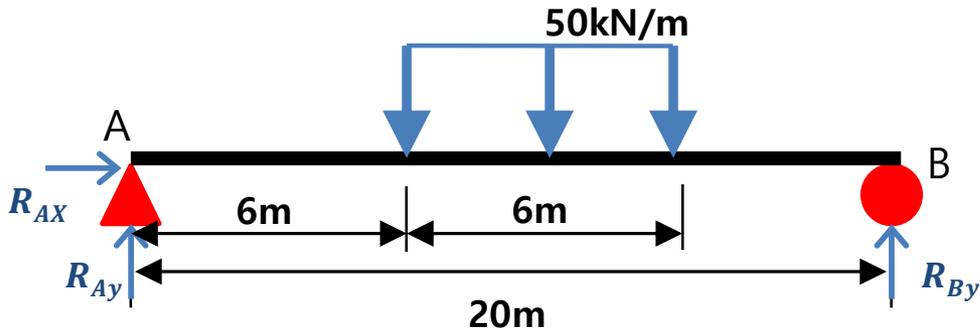
$$\rightarrow F_x = 0, R_{Ax} = 0$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

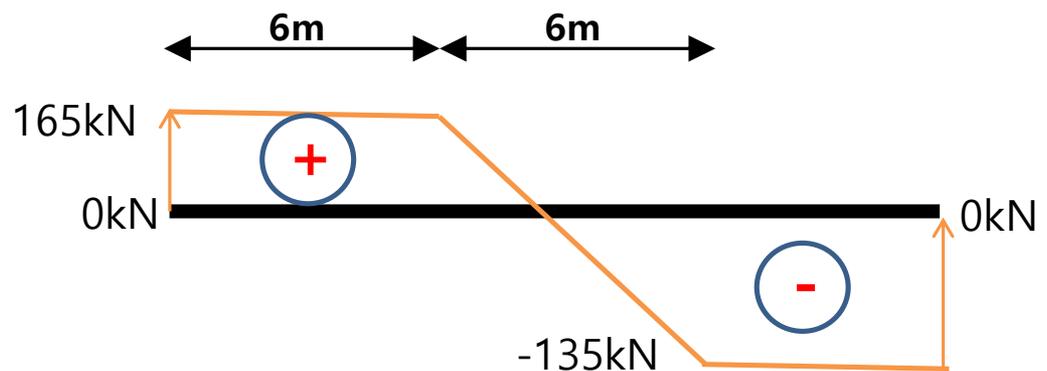
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 15)



$$M_A + \curvearrowright = 0, (50\text{kN} \times 6\text{m} \times (6+3)\text{m}) - (R_{By} \times 20\text{m}) = 0, R_{By} = 135\text{kN}$$

$$\uparrow F_y = 0, R_{Ay} + R_{By} = 300\text{kN}, R_{Ay} = 165\text{kN}$$

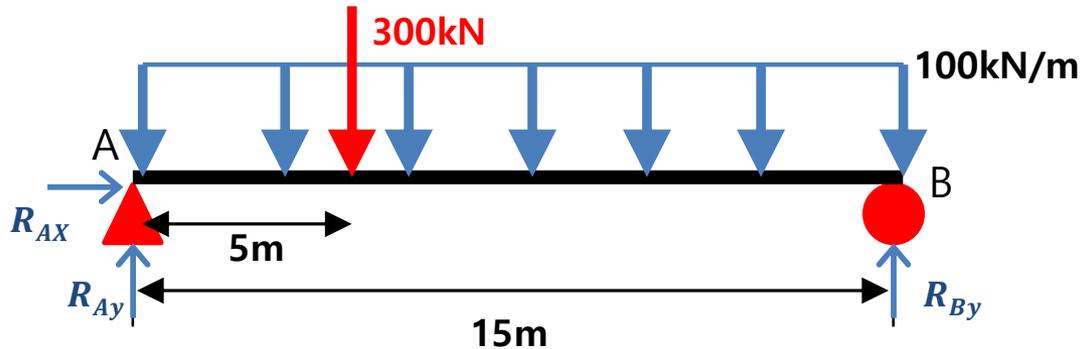
$$\rightarrow F_x = 0, R_{Ax} = 0$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

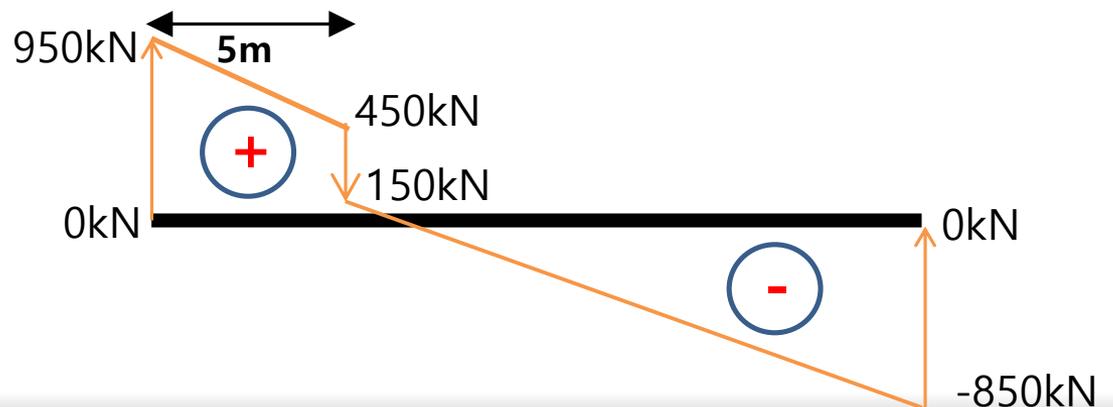
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 16)



$$M_A + \curvearrowright = 0, (100\text{kN} \times 15\text{m} \times 7.5\text{m}) + (300\text{kN} \times 5\text{m}) - (R_{By} \times 15\text{m}) = 0, R_{By} = 850\text{kN}$$

$$\uparrow F_y = 0, R_{Ay} + R_{By} = 1,500\text{kN} + 300\text{kN}, R_{Ay} = 950\text{kN}$$

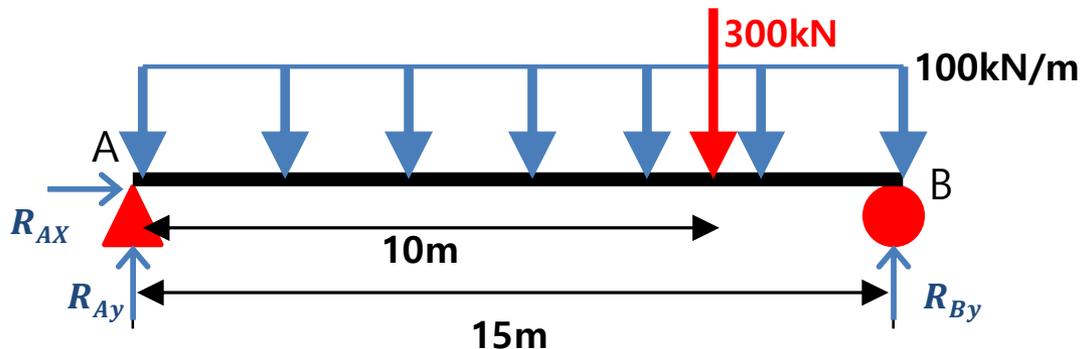
$$\rightarrow F_x = 0, R_{Ax} = 0$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

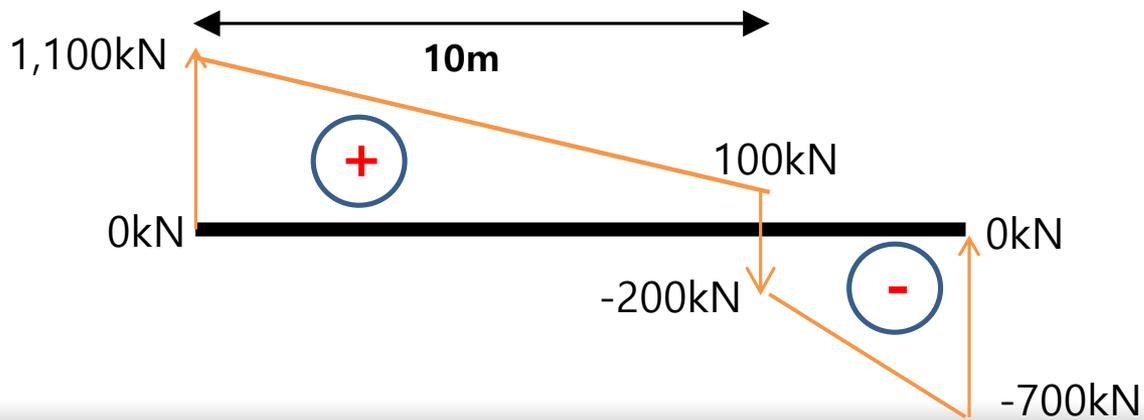
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 17)



$$M_A + \curvearrowright = 0, (100\text{kN} \times 15\text{m} \times 7.5\text{m}) + (300\text{kN} \times 10\text{m}) - (R_{By} \times 15\text{m}) = 0, R_{By} = 700\text{kN}$$

$$\uparrow F_y = 0, R_{Ay} + R_{By} = 1,500\text{kN} + 300\text{kN}, R_{Ay} = 1,100\text{kN}$$

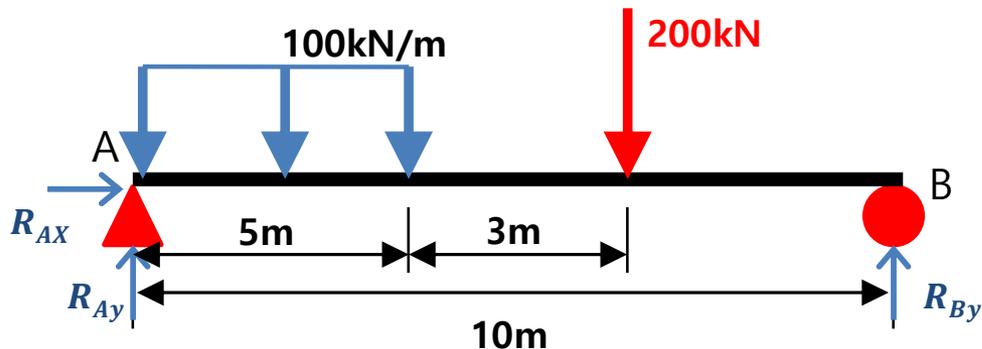
$$\rightarrow F_x = 0, R_{Ax} = 0$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

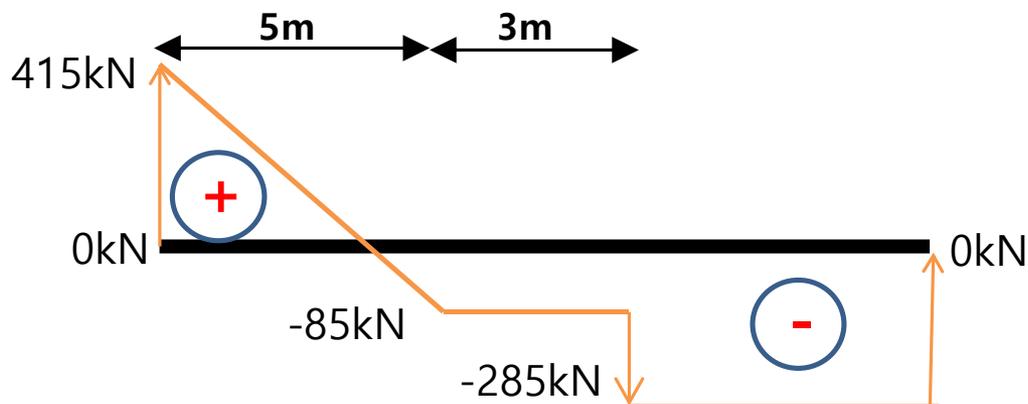
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 18)



$$M_A + \curvearrowright = 0, (100\text{kN} \times 5\text{m} \times 2.5\text{m}) + (200\text{kN} \times 8\text{m}) - (R_{By} \times 10\text{m}) = 0, R_{By} = 285\text{kN}$$

$$\uparrow F_y = 0, R_{Ay} + R_{By} = 700\text{kN}, R_{Ay} = 415\text{kN}$$

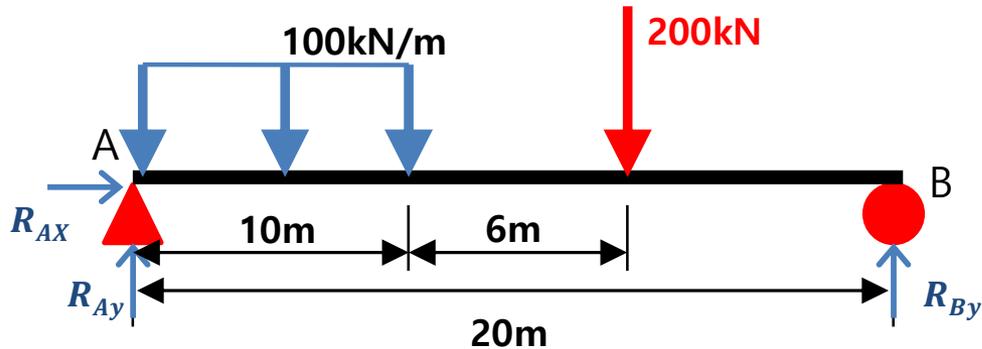
$$\rightarrow F_x = 0, R_{Ax} = 0$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

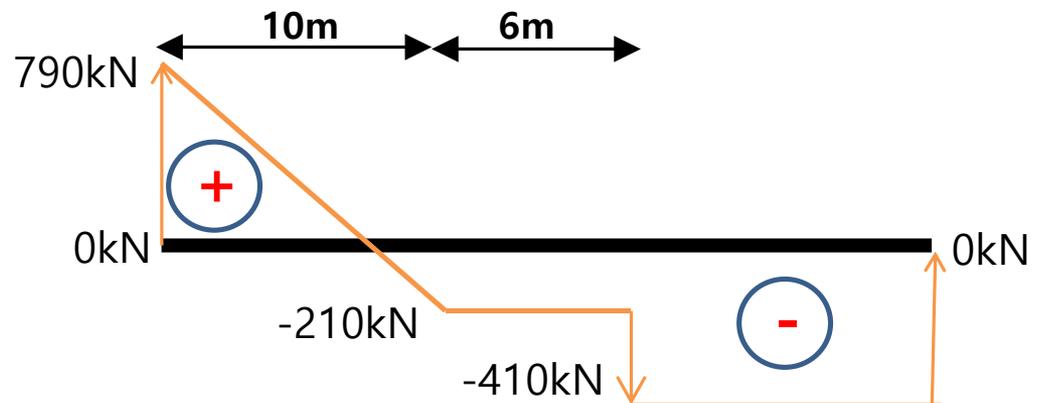
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 19)



$$M_A + \curvearrowright = 0, (100\text{kN} \times 10\text{m} \times 5\text{m}) + (200\text{kN} \times 16\text{m}) - (R_{By} \times 20\text{m}) = 0, R_{By} = 410\text{kN}$$

$$\uparrow F_y = 0, R_{Ay} + R_{By} = 1,000\text{kN} + 200\text{kN}, R_{Ay} = 790\text{kN}$$

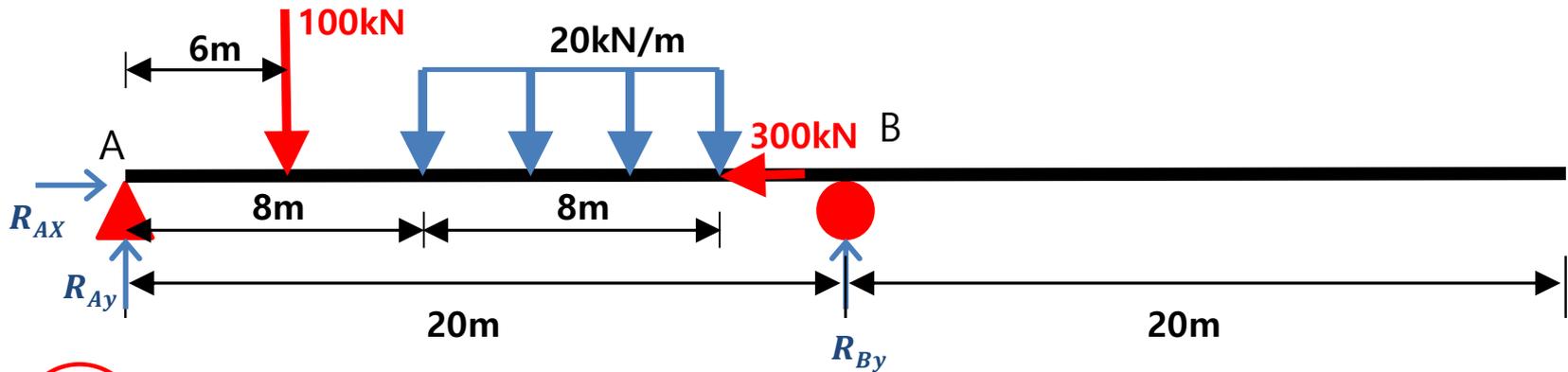
$$\rightarrow F_x = 0, R_{Ax} = 0$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

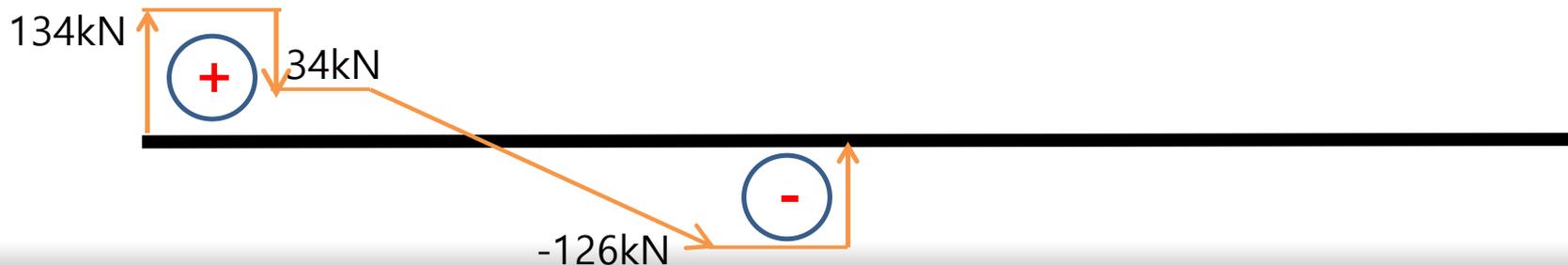
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 20)



$$M_A + \curvearrowright = 0, \quad (160\text{kN} \times (8+4)\text{m}) + (100\text{kN} \times 6\text{m}) - (R_{By} \times 20\text{m}) = 0, \quad R_{By} = 126\text{kN}$$

$$\uparrow F_y = 0, \quad R_{Ay} + R_{By} = 260\text{kN}, \quad R_{Ay} = 134\text{kN}$$

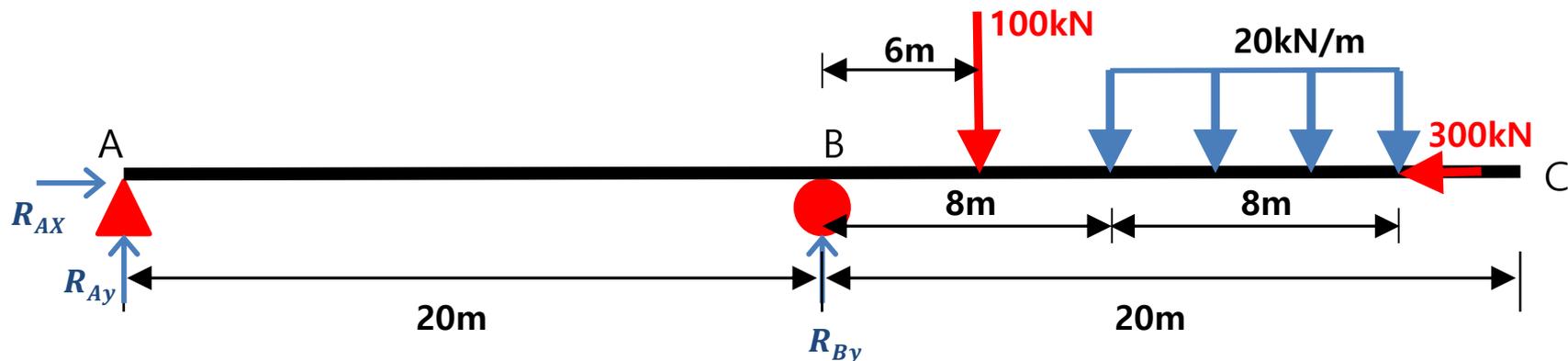
$$\rightarrow F_x = 0, \quad R_{AX} - 300\text{kN} = 0, \quad R_{AX} = 300\text{kN}$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

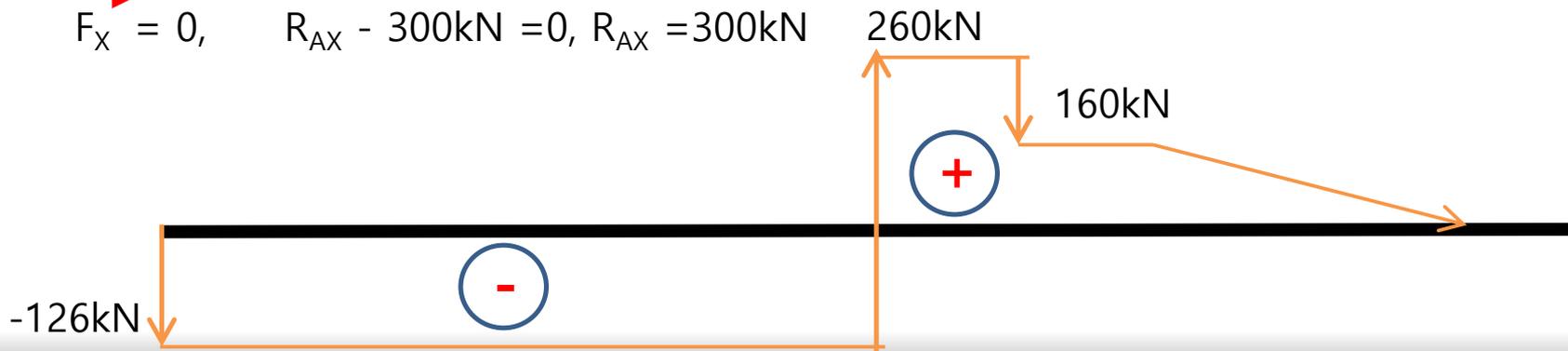
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 21)



$$M_A + \curvearrowright = 0, \quad (160\text{kN} \times (28+4)\text{m}) + (100\text{kN} \times (20+6)\text{m}) - (R_{By} \times 20\text{m}) = 0, \quad R_{By} = 386\text{kN}$$

$$\uparrow F_y = 0, \quad R_{Ay} + R_{By} = 260\text{kN}, \quad R_{Ay} = -126\text{kN}(\text{부반력})$$

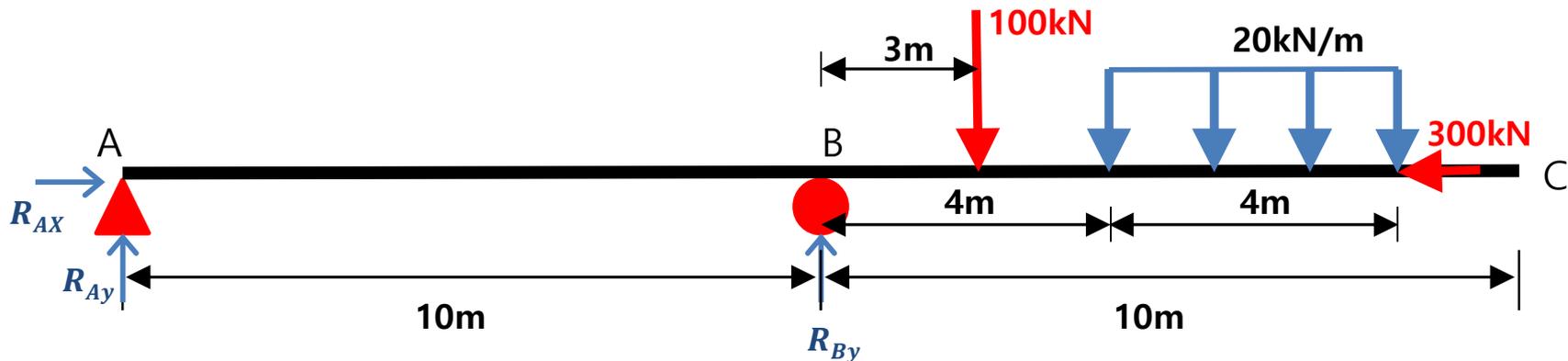
$$\rightarrow F_x = 0, \quad R_{Ax} - 300\text{kN} = 0, \quad R_{Ax} = 300\text{kN}$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 22)



$$M_A + \curvearrowright = 0, \quad (80\text{kN} \times (14+2)\text{m}) + (100\text{kN} \times (10+3)\text{m}) - (R_{By} \times 20\text{m}) = 0, \quad R_{By} = 129\text{kN}$$

$$\uparrow F_y = 0, \quad R_{Ay} + R_{By} = 180\text{kN}, \quad R_{Ay} = 51\text{kN}$$

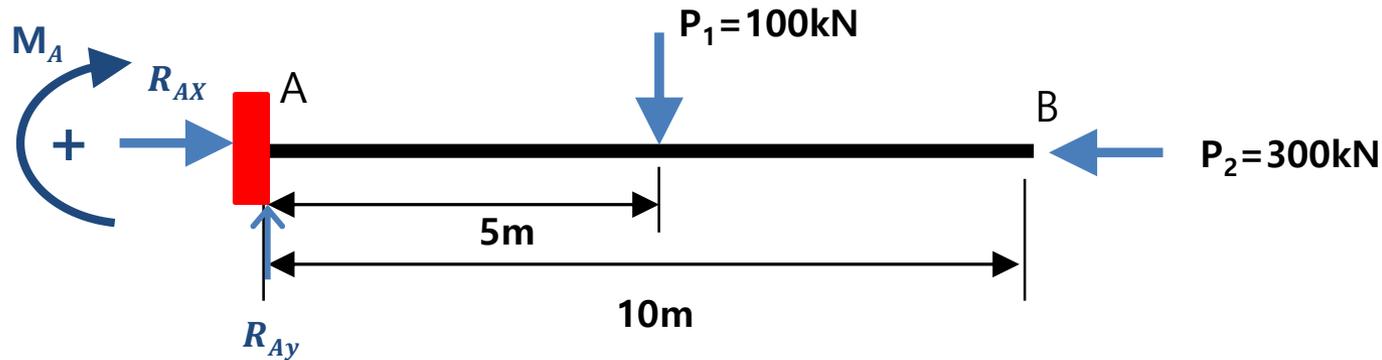
$$\rightarrow F_x = 0, \quad R_{Ax} - 300\text{kN} = 0, \quad R_{Ax} = 300\text{kN}$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

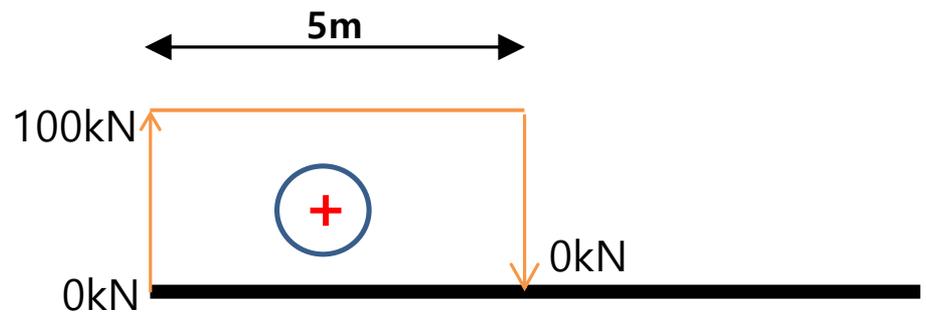
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 23)



$$M_A + \curvearrowright = 0, \quad M_A + (100\text{kN} \times 5\text{m}) = 0, \quad M_A = -500\text{kN}\cdot\text{m}$$

$$\uparrow F_y = 0, \quad R_{Ay} - 100\text{kN} = 0, \quad R_{Ay} = 100\text{kN}$$

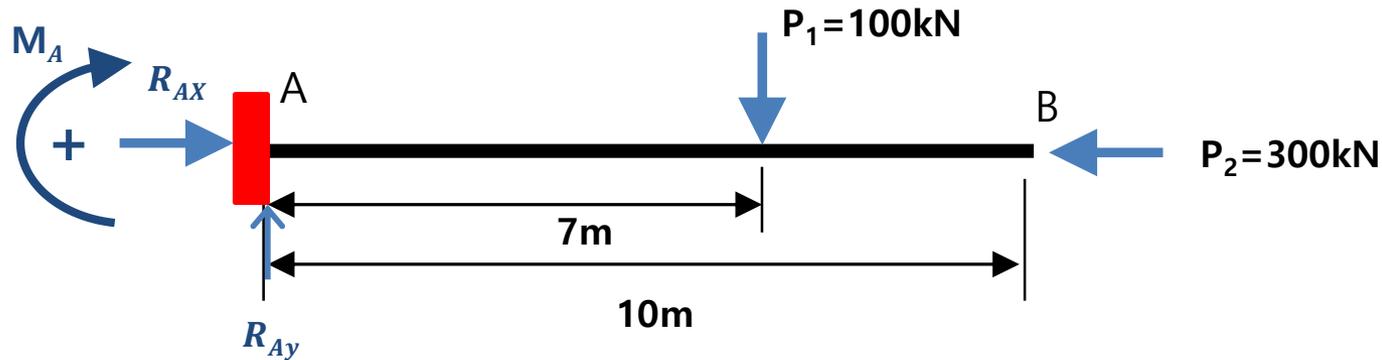
$$\rightarrow F_x = 0, \quad R_{Ax} - 300\text{kN} = 0, \quad R_{Ax} = 300\text{kN}$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

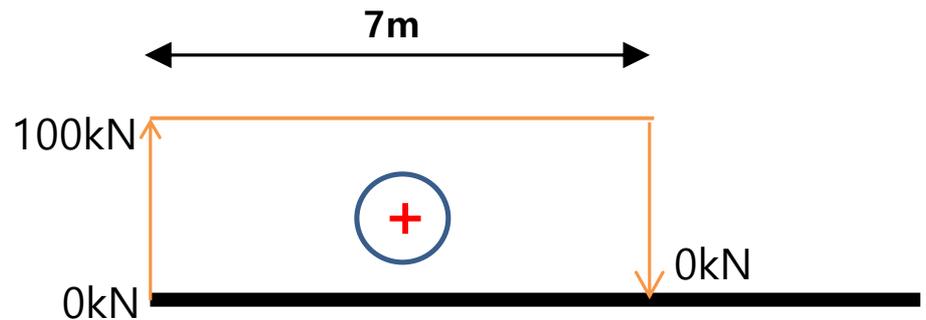
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 24)



$$M_A + \curvearrowright = 0, \quad M_A + (100\text{kN} \times 5\text{m}) = 0, \quad M_A = -500\text{kN}\cdot\text{m}$$

$$\uparrow F_y = 0, \quad R_{Ay} - 100\text{kN} = 0, \quad R_{Ay} = 100\text{kN}$$

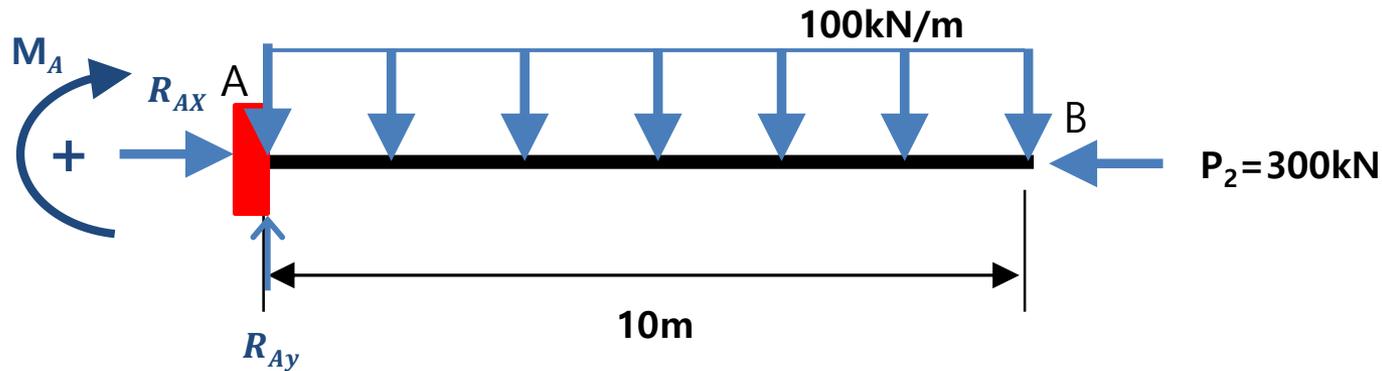
$$\rightarrow F_x = 0, \quad R_{Ax} - 300\text{kN} = 0, \quad R_{Ax} = 300\text{kN}$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

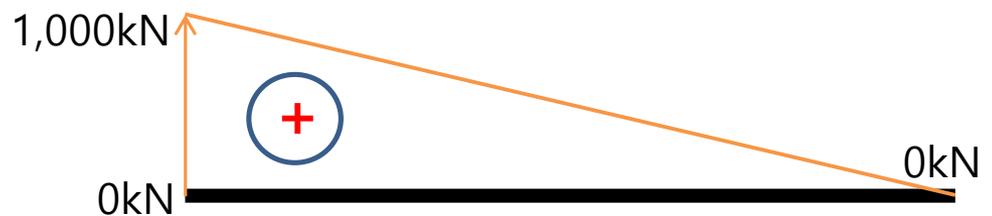
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 25)



$$M_A + \curvearrowright = 0, \quad M_A + (100\text{kN/m} \times 10\text{m} \times 5\text{m}) = 0, \quad M_A = -5,000\text{kN}\cdot\text{m}$$

$$\uparrow F_y = 0, \quad R_{Ay} - (100\text{kN/m} \times 10\text{m}) = 0, \quad R_{Ay} = 1,000\text{kN}$$

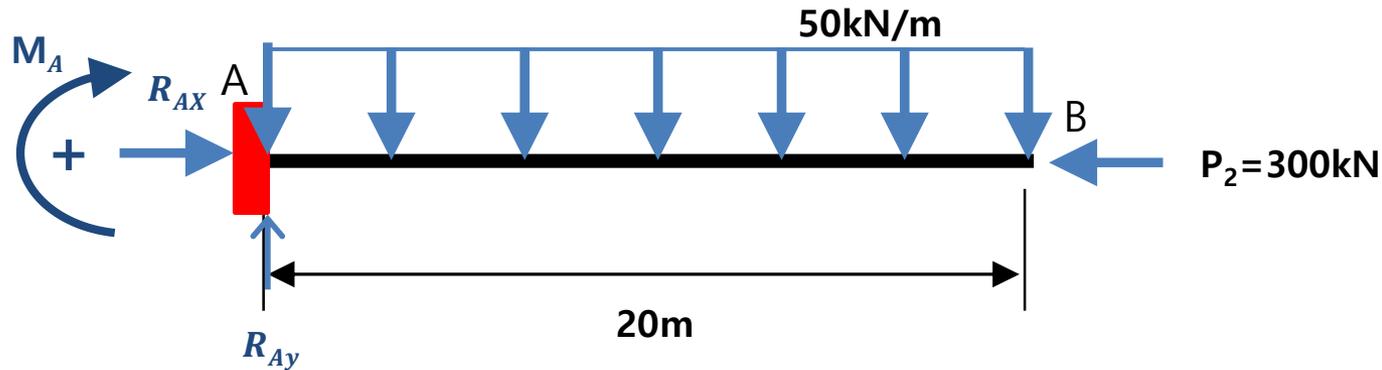
$$\rightarrow F_x = 0, \quad R_{AX} - 300\text{kN} = 0, \quad R_{AX} = 300\text{kN}$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

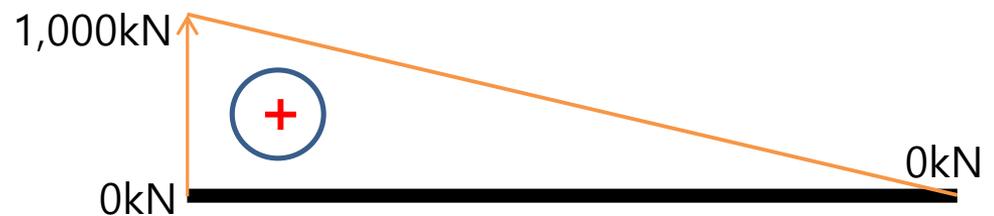
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 26)



$$M_A + \curvearrowright = 0, \quad M_A + (50\text{kN/m} \times 20\text{m} \times 10\text{m}) = 0, \quad M_A = -10,000\text{kN}\cdot\text{m}$$

$$\uparrow F_y = 0, \quad R_{Ay} - (50\text{kN/m} \times 20\text{m}) = 0, \quad R_{Ay} = 1,000\text{kN}$$

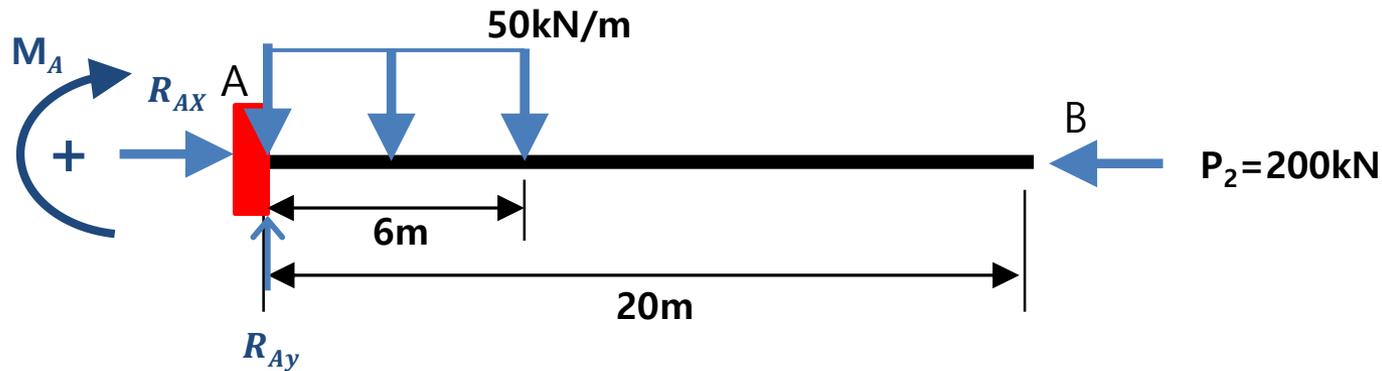
$$\rightarrow F_x = 0, \quad R_{AX} - 300\text{kN} = 0, \quad R_{AX} = 300\text{kN}$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

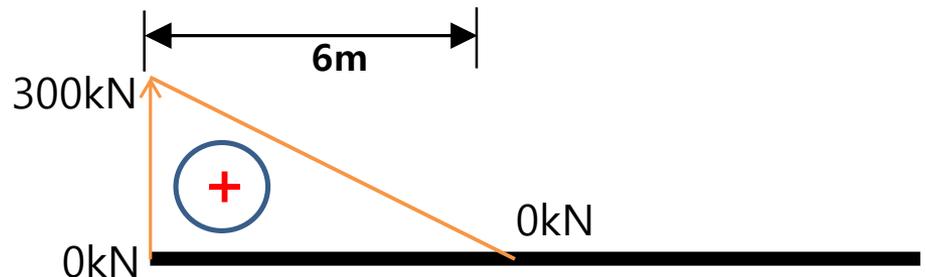
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 27)



$$M_A + \curvearrowright = 0, \quad M_A + (50\text{kN/m} \times 6\text{m} \times 3\text{m}) = 0, \quad M_A = -900\text{kN}\cdot\text{m}$$

$$\uparrow F_y = 0, \quad R_{Ay} - (50\text{kN/m} \times 6\text{m}) = 0, \quad R_{Ay} = 300\text{kN}$$

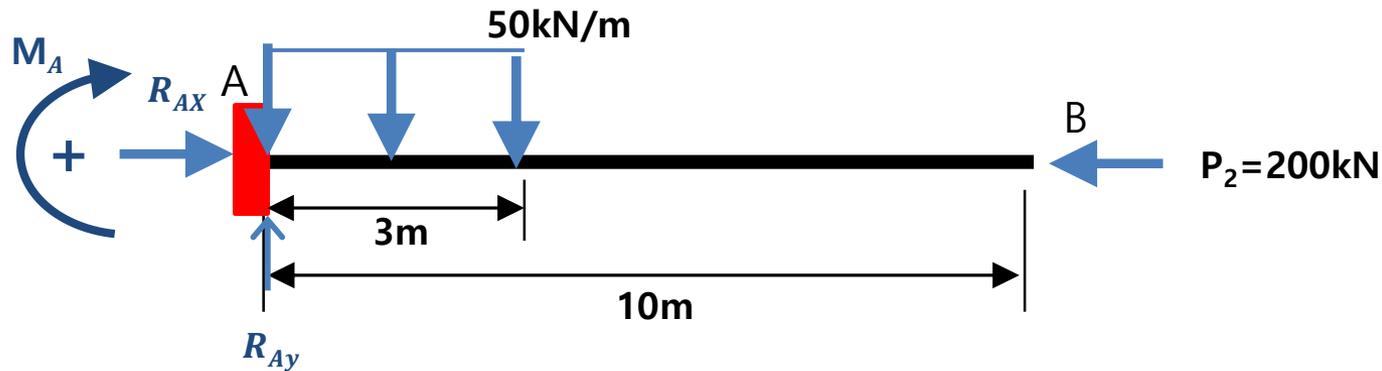
$$\rightarrow F_x = 0, \quad R_{Ax} - 200\text{kN} = 0, \quad R_{Ax} = 200\text{kN}$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

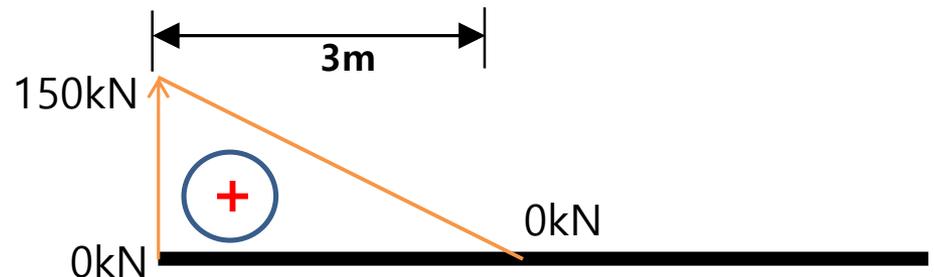
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 28)



$$\overset{\curvearrowright}{M_A} + \uparrow = 0, \quad M_A + (50\text{kN/m} \times 3\text{m} \times 1.5\text{m}) = 0, \quad M_A = -225\text{kN}\cdot\text{m}$$

$$\uparrow F_y = 0, \quad R_{Ay} - (50\text{kN/m} \times 3\text{m}) = 0, \quad R_{Ay} = 150\text{kN}$$

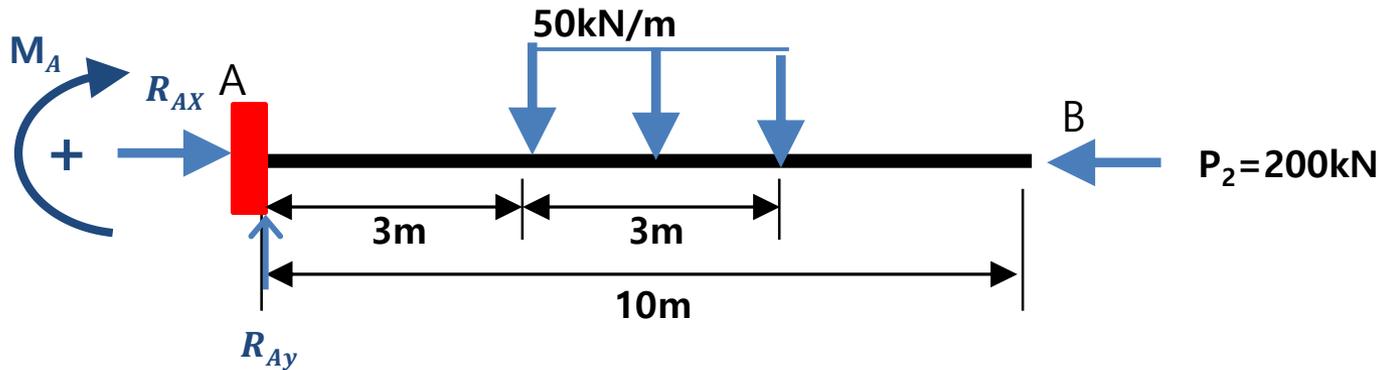
$$\rightarrow F_x = 0, \quad R_{Ax} - 200\text{kN} = 0, \quad R_{Ax} = 200\text{kN}$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

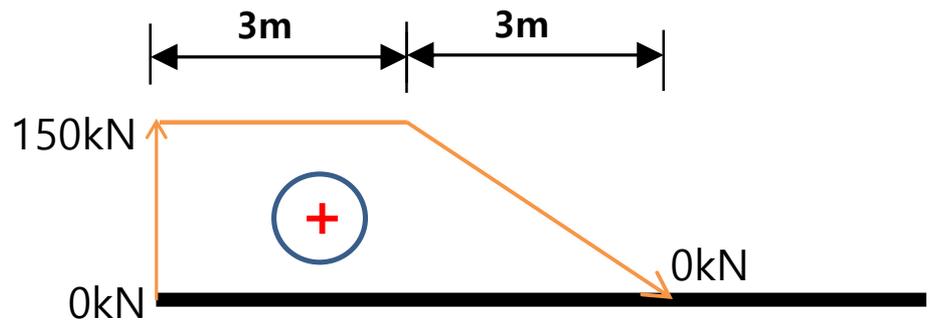
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 29)



$$\overset{\curvearrowright}{M_A} + \uparrow = 0, \quad M_A + (50\text{kN/m} \times 3\text{m} \times (3+1.5)\text{m}) = 0, \quad M_A = -675\text{kN}\cdot\text{m}$$

$$\uparrow F_y = 0, \quad R_{Ay} - (50\text{kN/m} \times 3\text{m}) = 0, \quad R_{Ay} = 150\text{kN}$$

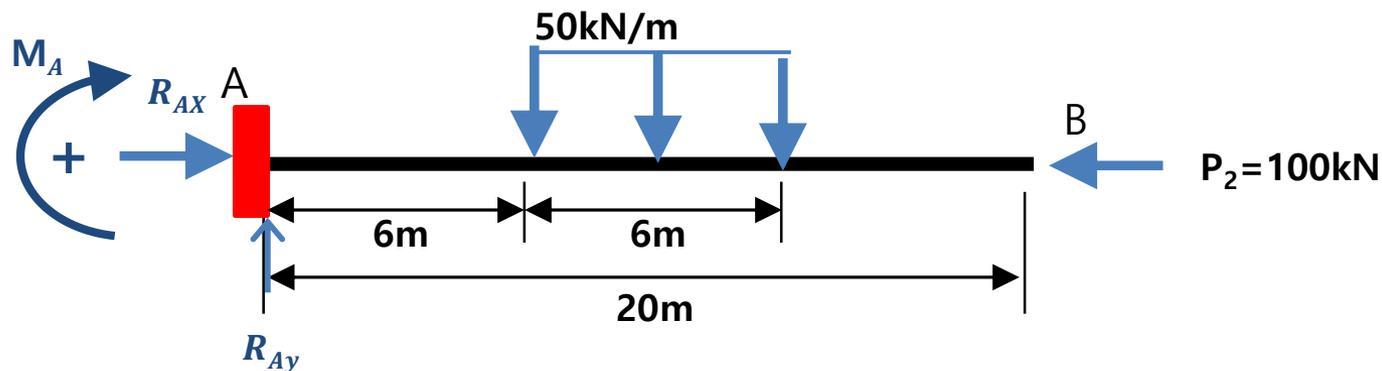
$$\rightarrow F_x = 0, \quad R_{Ax} - 200\text{kN} = 0, \quad R_{Ax} = 200\text{kN}$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

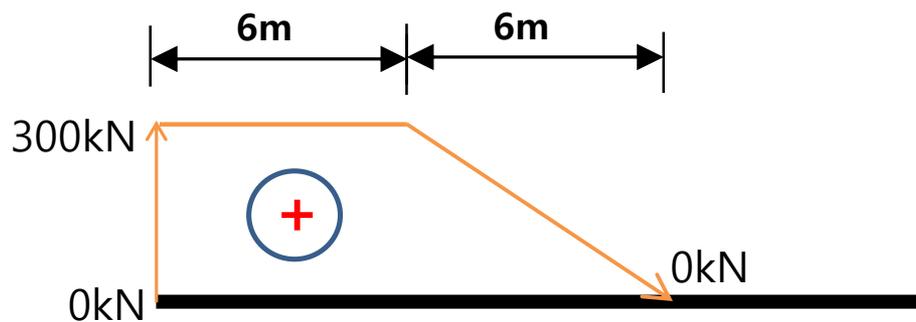
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 30)



$$\overset{\curvearrowright}{M_A} + \uparrow = 0, \quad M_A + (50\text{kN/m} \times 6\text{m} \times (6+3)\text{m}) = 0, \quad M_A = -2,700\text{kN}\cdot\text{m}$$

$$\uparrow F_y = 0, \quad R_{Ay} - (50\text{kN/m} \times 6\text{m}) = 0, \quad R_{Ay} = 300\text{kN}$$

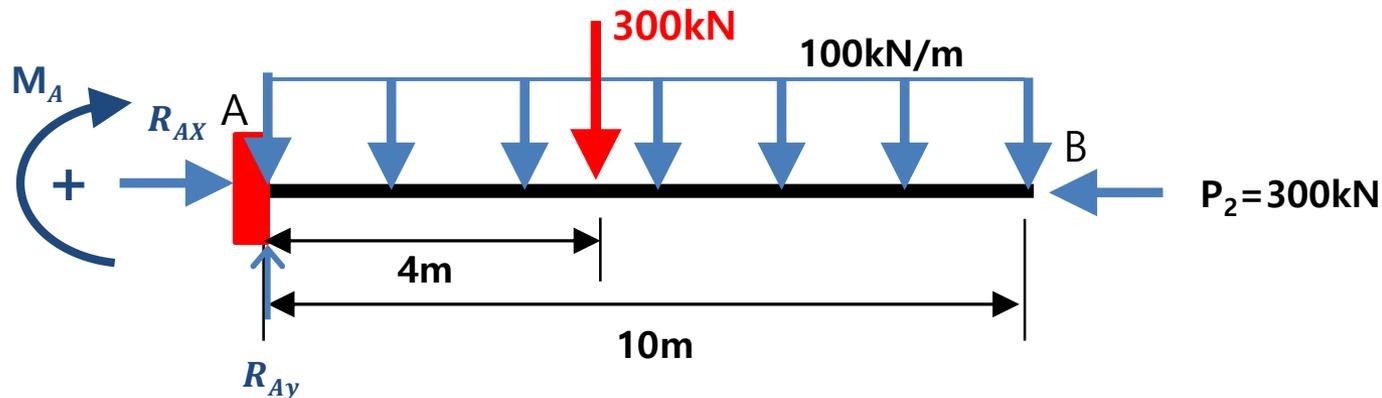
$$\rightarrow F_x = 0, \quad R_{Ax} - 100\text{kN} = 0, \quad R_{Ax} = 100\text{kN}$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

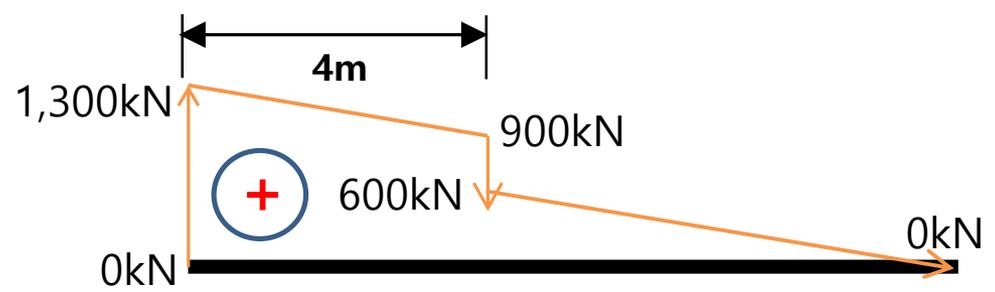
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 31)



$$\overset{\curvearrowright}{M_A} + \uparrow = 0, \quad M_A + (100\text{kN/m} \times 10\text{m} \times 5\text{m}) + (300\text{kN} \times 4\text{m}) = 0, \quad M_A = -6,200\text{kN}\cdot\text{m}$$

$$\uparrow F_y = 0, \quad R_{Ay} - (100\text{kN/m} \times 10\text{m}) - 300\text{kN} = 0, \quad R_{Ay} = 1,300\text{kN}$$

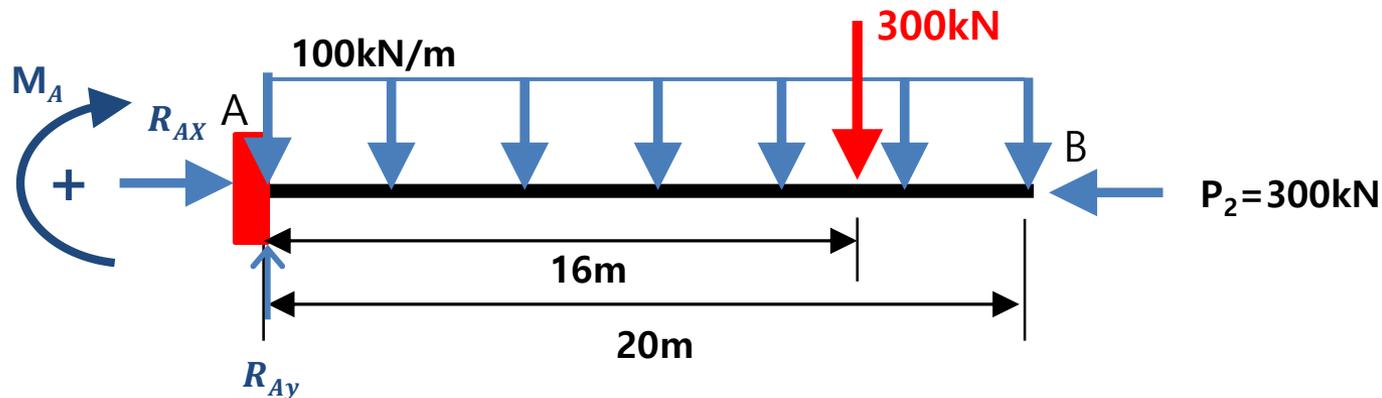
$$\rightarrow F_x = 0, \quad R_{Ax} - 300\text{kN} = 0, \quad R_{Ax} = 300\text{kN}$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

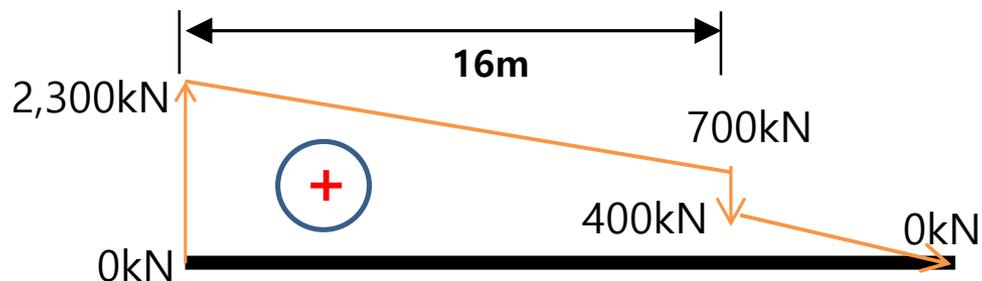
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 32)



$$\overset{\curvearrowright}{M_A} + \uparrow = 0, \quad M_A + (100\text{kN/m} \times 20\text{m} \times 10\text{m}) + (300\text{kN} \times 16\text{m}) = 0, \quad M_A = -24,800\text{kN}\cdot\text{m}$$

$$\uparrow F_y = 0, \quad R_{Ay} - (100\text{kN/m} \times 20\text{m}) - 300\text{kN} = 0, \quad R_{Ay} = 2,300\text{kN}$$

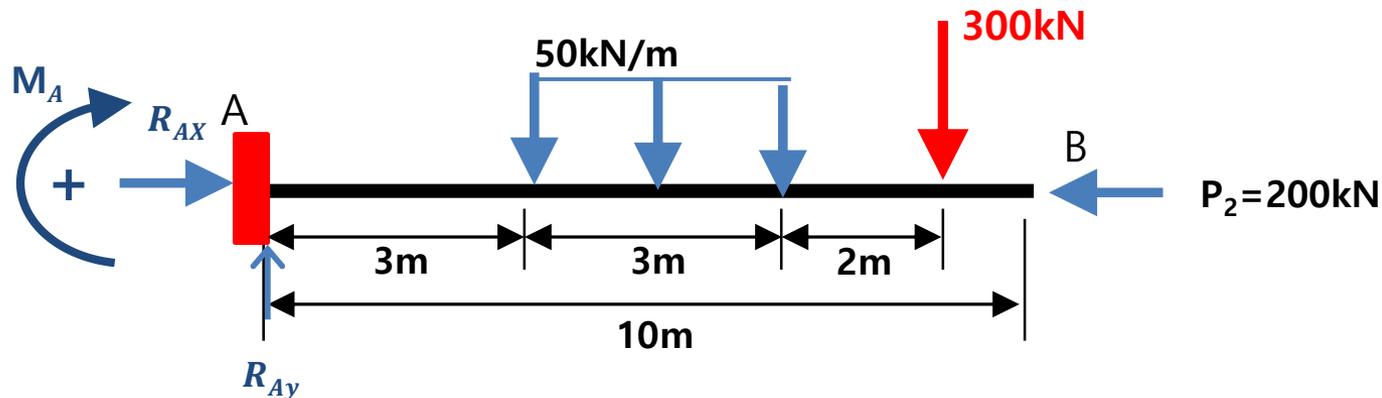
$$\rightarrow F_x = 0, \quad R_{AX} - 300\text{kN} = 0, \quad R_{AX} = 300\text{kN}$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

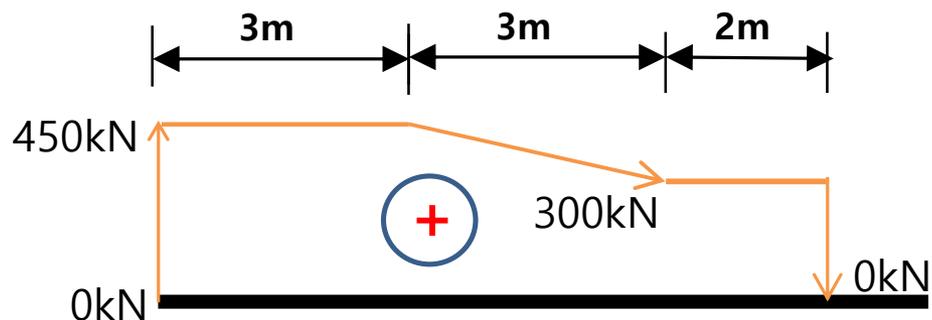
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 33)



$$M_A + \curvearrowright = 0, \quad M_A + (50\text{kN/m} \times 3\text{m} \times (3+1.5)\text{m}) + (300\text{kN} \times 8\text{m}) = 0, \quad M_A = -3,075\text{kN}\cdot\text{m}$$

$$\uparrow F_y = 0, \quad R_{Ay} - (50\text{kN/m} \times 3\text{m}) - 300\text{kN} = 0, \quad R_{Ay} = 450\text{kN}$$

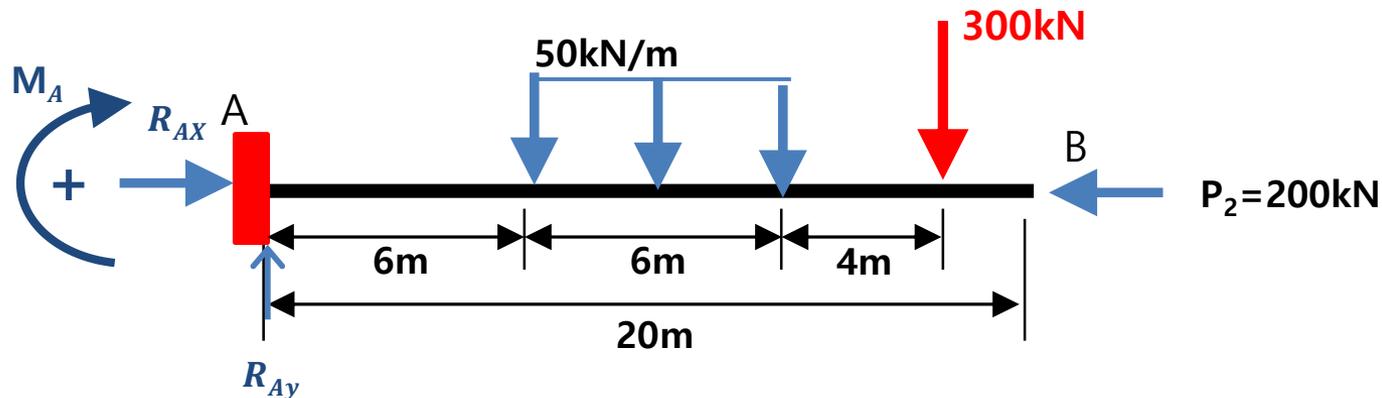
$$\rightarrow F_x = 0, \quad R_{Ax} - 200\text{kN} = 0, \quad R_{Ax} = 200\text{kN}$$



# I. 보의 휨응력과 전단응력

## I.2 전단력도 (Shear Force Diagram ; S. F. D)

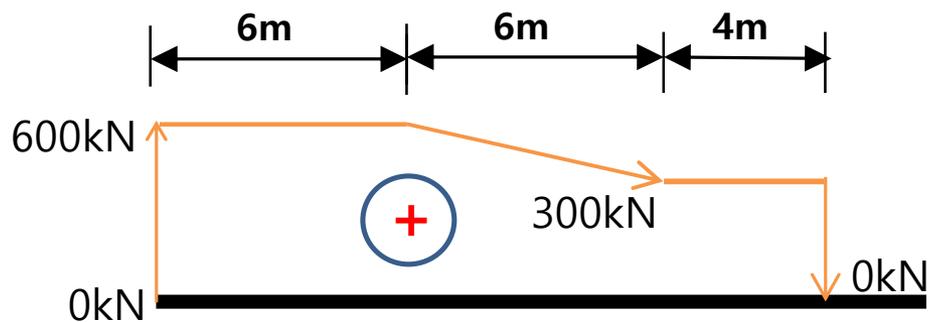
- 구조물 부재 각 단면의 전단력을 나타내는 선도 (예제 34)



$$\overset{\curvearrowright}{M_A} + \uparrow = 0, \quad M_A + (50\text{kN/m} \times 6\text{m} \times (6+3)\text{m}) + (300\text{kN} \times 16\text{m}) = 0, \quad M_A = -7,500\text{kN}\cdot\text{m}$$

$$\uparrow F_y = 0, \quad R_{Ay} - (50\text{kN/m} \times 6\text{m}) - 300\text{kN} = 0, \quad R_{Ay} = 600\text{kN}$$

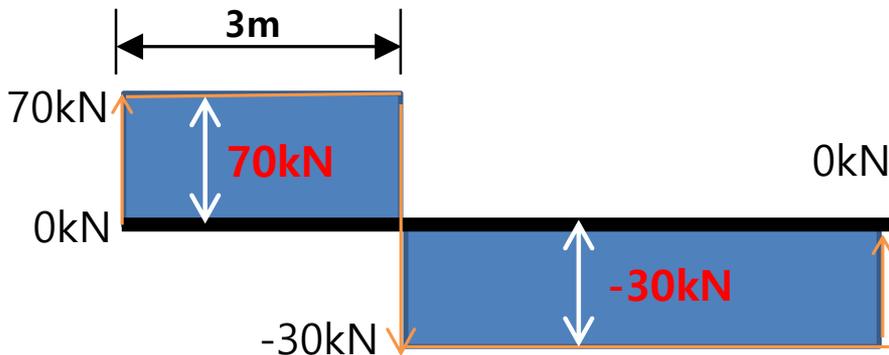
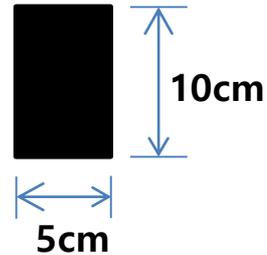
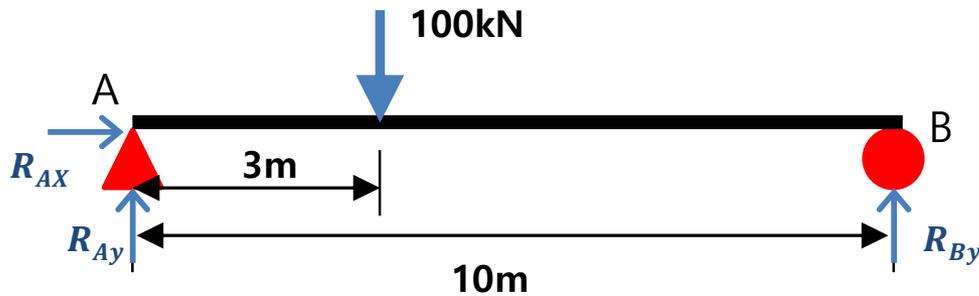
$$\rightarrow F_x = 0, \quad R_{Ax} - 200\text{kN} = 0, \quad R_{Ax} = 200\text{kN}$$



# I. 보의 휨응력과 전단응력

## I.2 전단 응력 (Shear Stress)

$$\tau = \frac{SQ}{Ib} \quad - \quad I : 2차 모멘트, b : 단면폭, S : 전단력, Q : 1차 모멘트$$



$$- \quad I = \frac{bh^3}{12} = \frac{(0.05)(0.1)^3}{12} = 0.000004166\text{m}^4$$

$$- \quad b = 0.05\text{m}$$

$$- \quad Q = \frac{bh^2}{2} = \frac{(0.05)(0.1)^2}{2} = 0.00025\text{m}^3$$

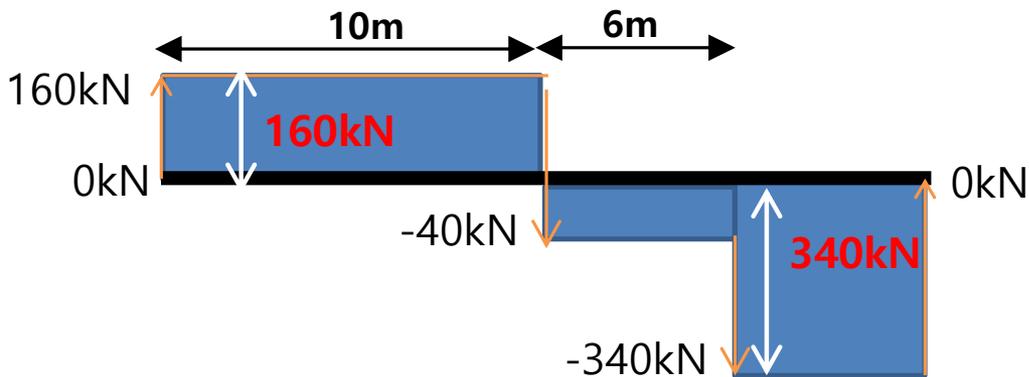
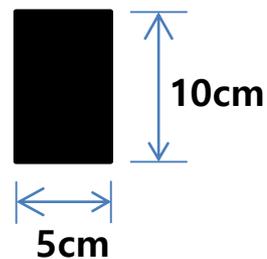
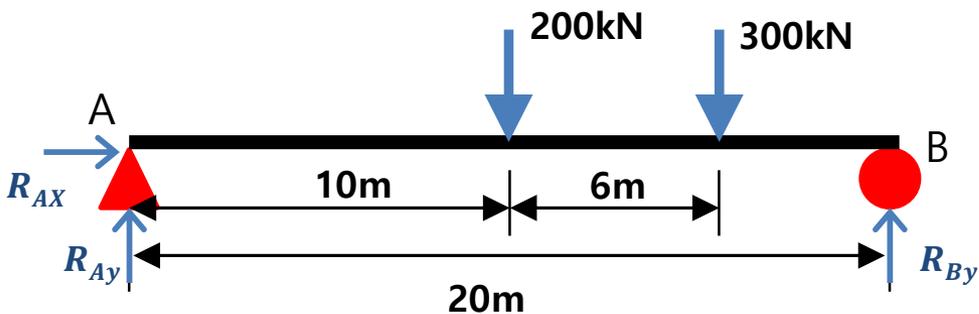
$$\tau = \frac{SQ}{Ib} = \frac{(70)(0.00025)}{(0.000004166)(0.05)} = 84,013 \text{ kN/m}^2$$

$$\tau = \frac{SQ}{Ib} = \frac{(-30)(0.00025)}{(0.000004166)(0.05)} = -36,005 \text{ kN/m}^2$$

# I. 보의 휨응력과 전단응력

## I.2 전단 응력 (Shear Stress)

$$\tau = \frac{SQ}{Ib} \quad - \quad I : 2차 모멘트, b : 단면폭, S : 전단력, Q : 1차 모멘트$$



$$I = \frac{bh^3}{12} = \frac{(0.05)(0.1)^3}{12} = 0.000004166\text{m}^4$$

$$b = 0.05\text{m}$$

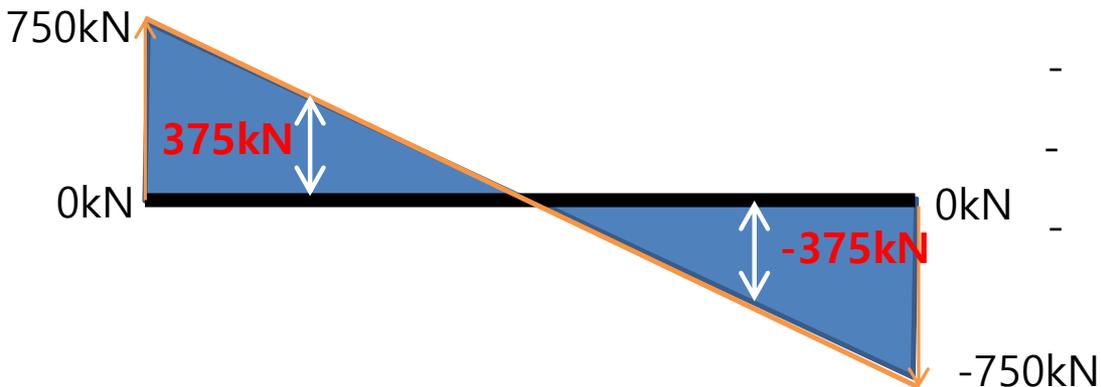
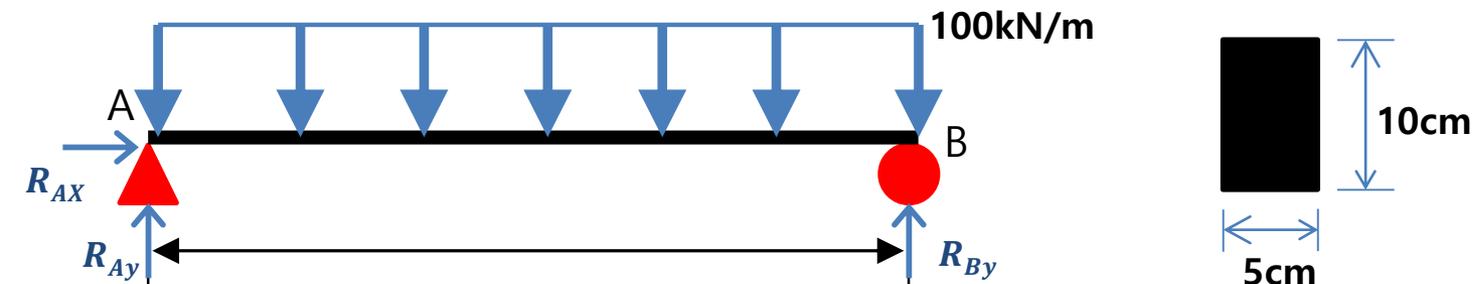
$$Q = \frac{bh^2}{2} = \frac{(0.05)(0.1)^2}{2} = 0.00025\text{m}^3$$

$$\tau = \frac{SQ}{Ib} = \frac{(160)(0.00025)}{(0.000004166)(0.05)} = 192,030 \text{ kN/m}^2 \quad \tau = \frac{SQ}{Ib} = \frac{(-340)(0.00025)}{(0.000004166)(0.05)} = -408,065 \text{ kN/m}^2$$

# I. 보의 휨응력과 전단응력

## I.2 전단 응력 (Shear Stress)

$$\tau = \frac{SQ}{Ib} \quad - \quad I : 2차 모멘트, b : 단면폭, S : 전단력, Q : 1차 모멘트$$



$$- \quad I = \frac{bh^3}{12} = \frac{(0.05)(0.1)^3}{12} = 0.000004166m^4$$

$$- \quad b = 0.05m$$

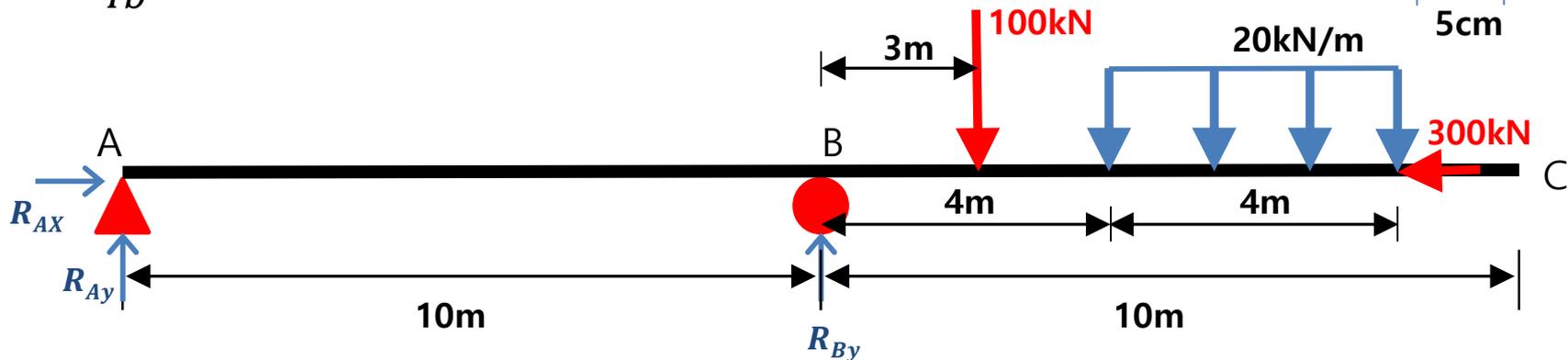
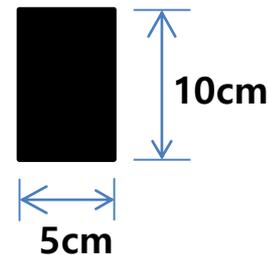
$$- \quad Q = \frac{bh^2}{2} = \frac{(0.05)(0.1)^2}{2} = 0.00025m^3$$

$$\tau = \frac{SQ}{Ib} = \frac{(375)(0.00025)}{(0.000004166)(0.05)} = 450,072 \text{ kN/m}^2 \quad \tau = \frac{SQ}{Ib} = \frac{(-375)(0.00025)}{(0.000004166)(0.05)} = -450,072 \text{ kN/m}^2$$

# I. 보의 휨응력과 전단응력

## I.2 전단 응력 (Shear Stress)

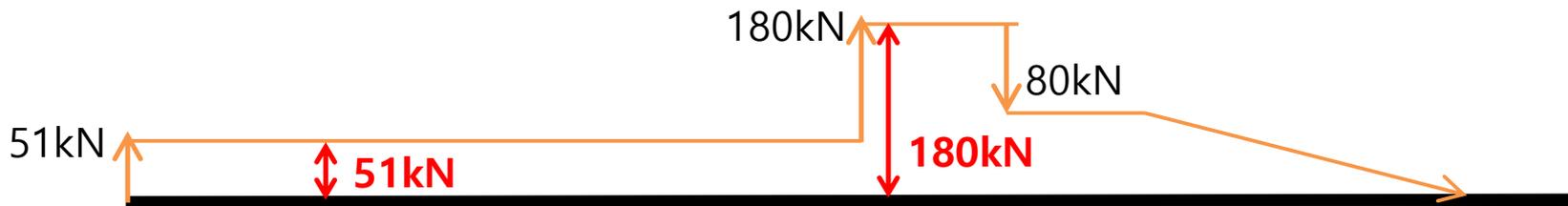
$$\tau = \frac{SQ}{Ib} \quad - \quad I : 2차 모멘트, b : 단면폭, S : 전단력, Q : 1차 모멘트$$



$$I = \frac{bh^3}{12} = \frac{(0.05)(0.1)^3}{12} = 0.000004166m^4$$

$$b = 0.05m$$

$$Q = \frac{bh^2}{2} = \frac{(0.05)(0.1)^2}{2} = 0.00025m^3$$



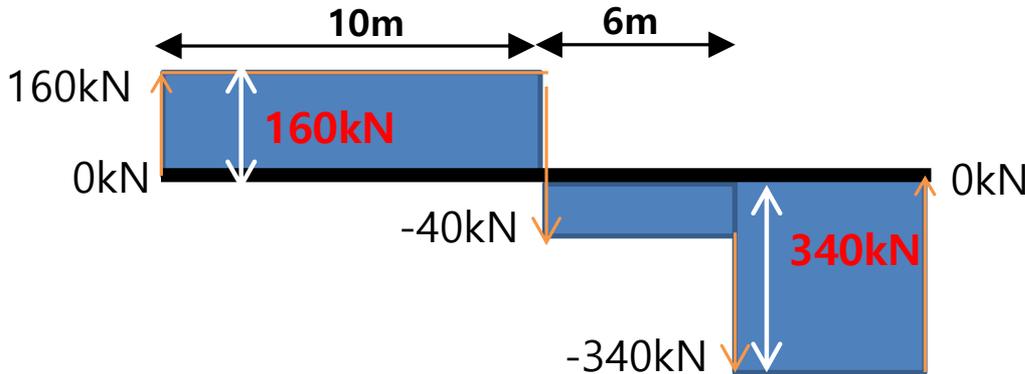
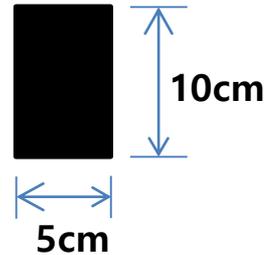
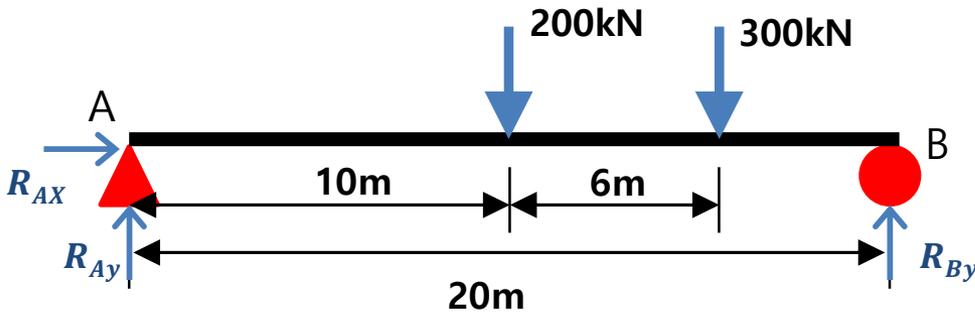
$$\tau = \frac{SQ}{Ib} = \frac{(51)(0.00025)}{(0.000004166)(0.05)} = 61,209 \text{ kN/m}^2$$

$$\tau = \frac{SQ}{Ib} = \frac{(180)(0.00025)}{(0.000004166)(0.05)} = 216,034 \text{ kN/m}^2$$

# I. 보의 휨응력과 전단응력

## I.2 전단 응력 (Shear Stress)

$$\tau = \frac{SQ}{Ib} \quad - \quad I : 2차 모멘트, b : 단면폭, S : 전단력, Q : 1차 모멘트$$



$$- \quad I = \frac{bh^3}{12} = \frac{(0.05)(0.1)^3}{12} = 0.000004166m^4$$

$$- \quad b = 0.05m$$

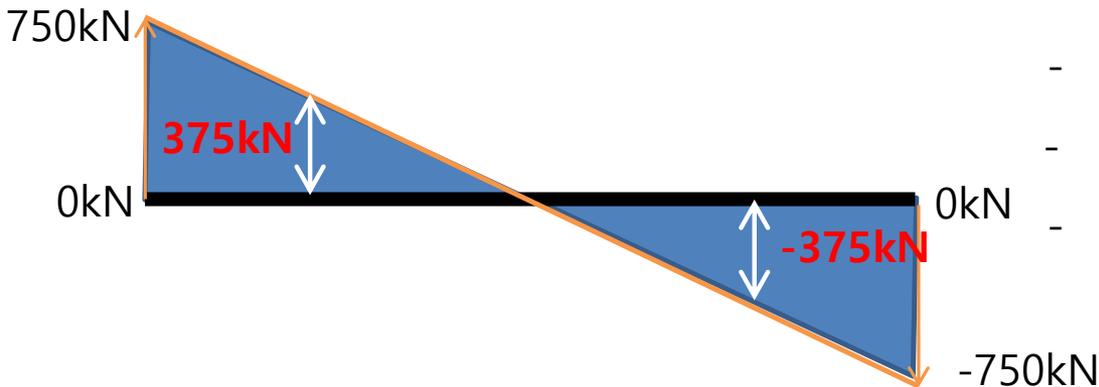
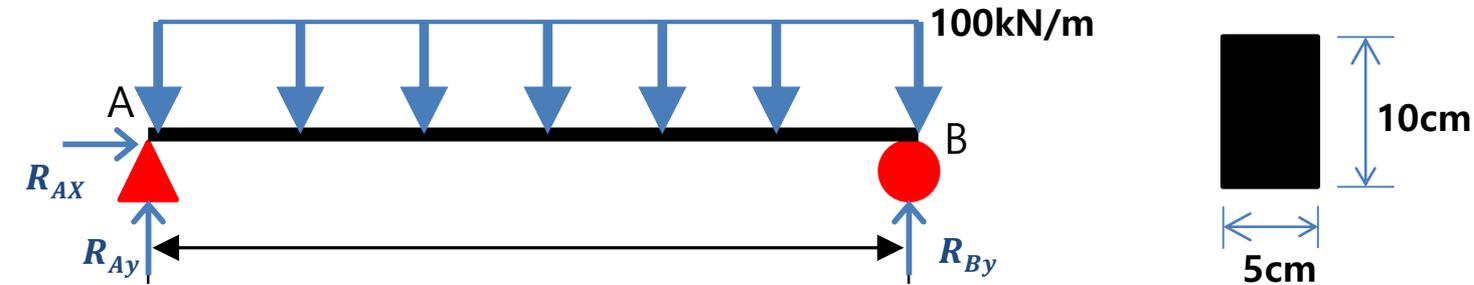
$$- \quad Q = \frac{bh^2}{2} = \frac{(0.05)(0.1)^2}{2} = 0.00025m^3$$

$$\tau = \frac{SQ}{Ib} = \frac{(160)(0.00025)}{(0.000004166)(0.05)} = 192,030 \text{ kN/m}^2 \quad \tau = \frac{SQ}{Ib} = \frac{(-340)(0.00025)}{(0.000004166)(0.05)} = -408,065 \text{ kN/m}^2$$

# I. 보의 휨응력과 전단응력

## I.2 전단 응력 (Shear Stress)

$$\tau = \frac{SQ}{Ib} \quad - \quad I : 2차 모멘트, b : 단면폭, S : 전단력, Q : 1차 모멘트$$



$$- \quad I = \frac{bh^3}{12} = \frac{(0.05)(0.1)^3}{12} = 0.000004166\text{m}^4$$

$$- \quad b = 0.05\text{m}$$

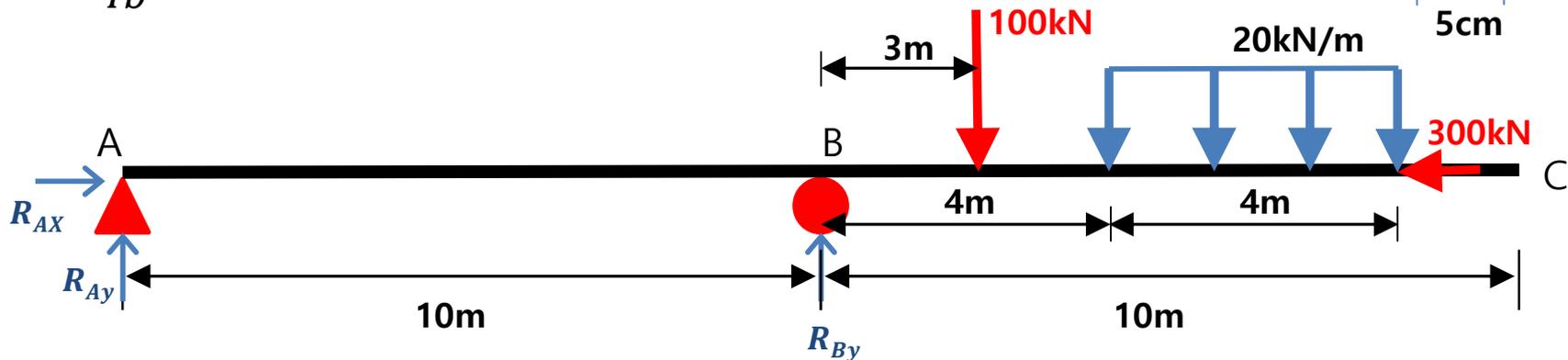
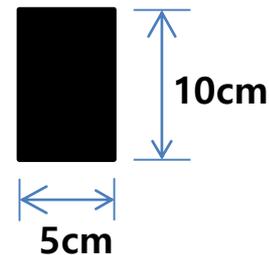
$$- \quad Q = \frac{bh^2}{2} = \frac{(0.05)(0.1)^2}{2} = 0.00025\text{m}^3$$

$$\tau = \frac{SQ}{Ib} = \frac{(375)(0.00025)}{(0.000004166)(0.05)} = 450,072 \text{ kN/m}^2 \quad \tau = \frac{SQ}{Ib} = \frac{(-375)(0.00025)}{(0.000004166)(0.05)} = -450,072 \text{ kN/m}^2$$

# I. 보의 휨응력과 전단응력

## I.2 전단 응력 (Shear Stress)

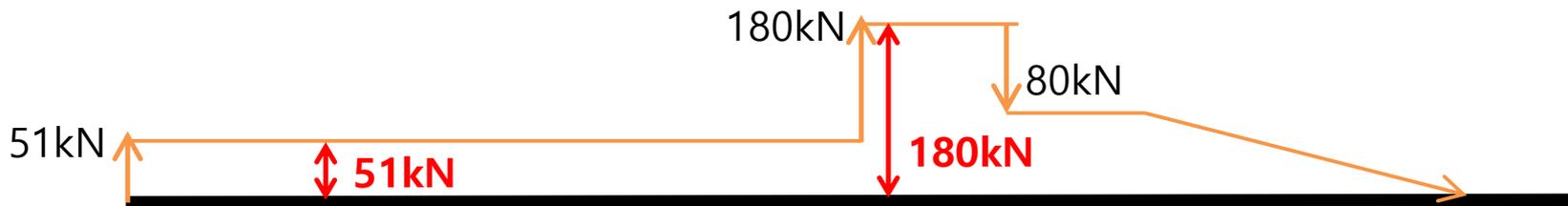
$$\tau = \frac{SQ}{Ib} \quad - \quad I : 2차 모멘트, b : 단면폭, S : 전단력, Q : 1차 모멘트$$



$$I = \frac{bh^3}{12} = \frac{(0.05)(0.1)^3}{12} = 0.000004166m^4$$

$$b = 0.05m$$

$$Q = \frac{bh^2}{2} = \frac{(0.05)(0.1)^2}{2} = 0.00025m^3$$



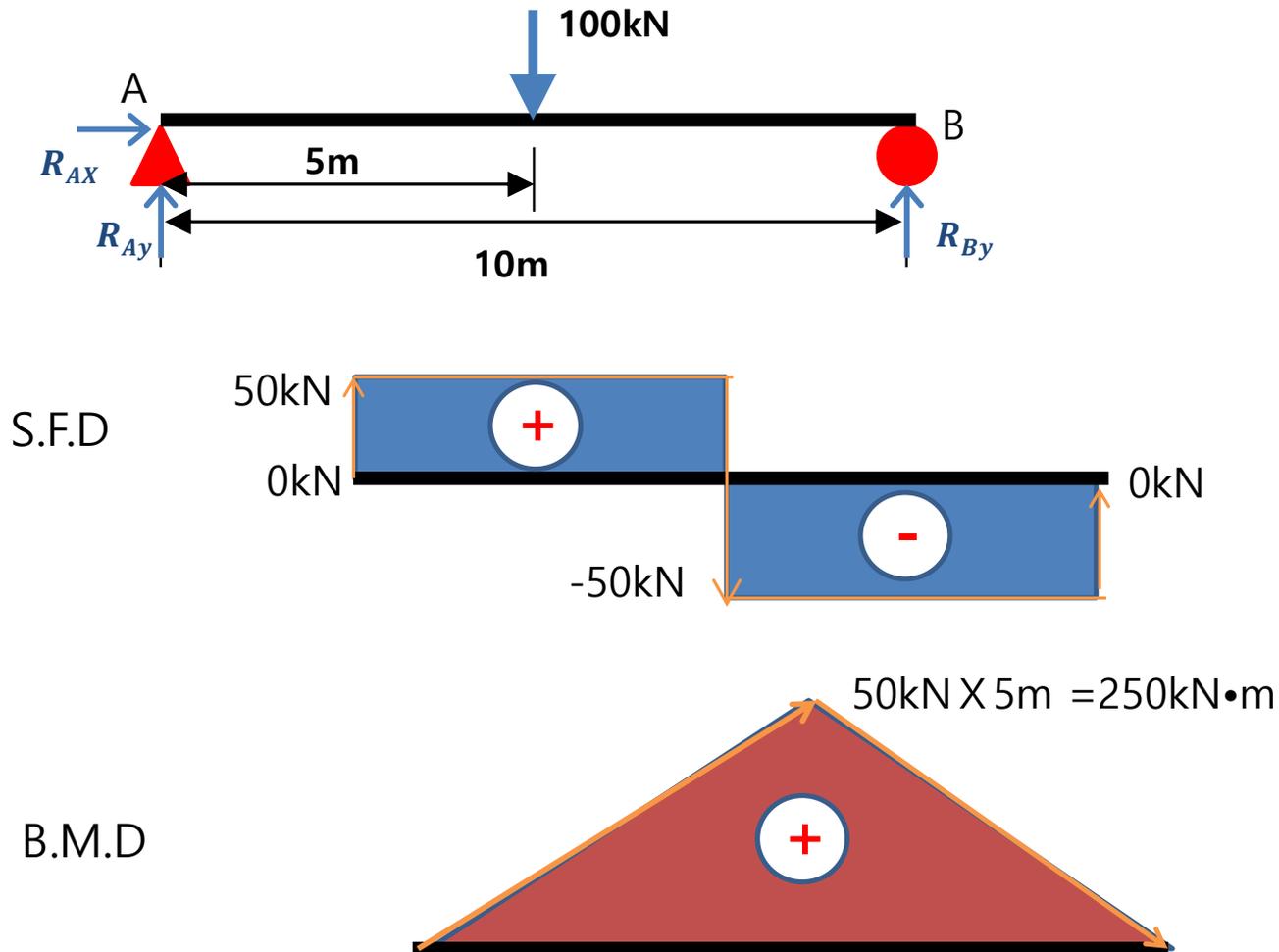
$$\tau = \frac{SQ}{Ib} = \frac{(51)(0.00025)}{(0.000004166)(0.05)} = 61,209 \text{ kN/m}^2$$

$$\tau = \frac{SQ}{Ib} = \frac{(180)(0.00025)}{(0.000004166)(0.05)} = 216,034 \text{ kN/m}^2$$

# I. 보의 휨응력과 전단응력

## I.3 휨모멘트도 (Bending Moment Diagram : B. M. D)

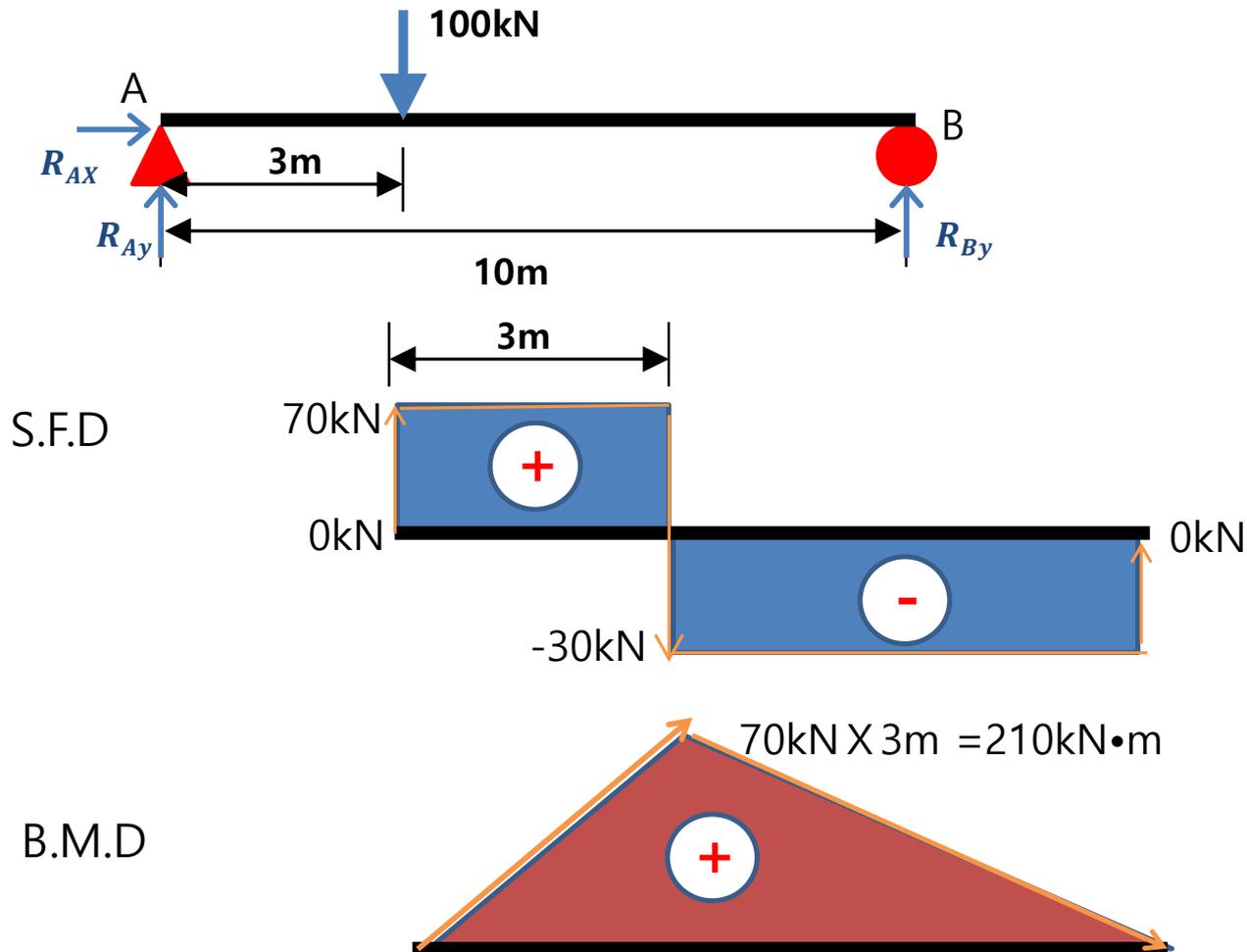
- 구조물 부재 각 단면의 휨모멘트를 나타내는 선도 (예제 1)



# I. 보의 휨응력과 전단응력

## I.3 휨모멘트도 (Bending Moment Diagram : B. M. D)

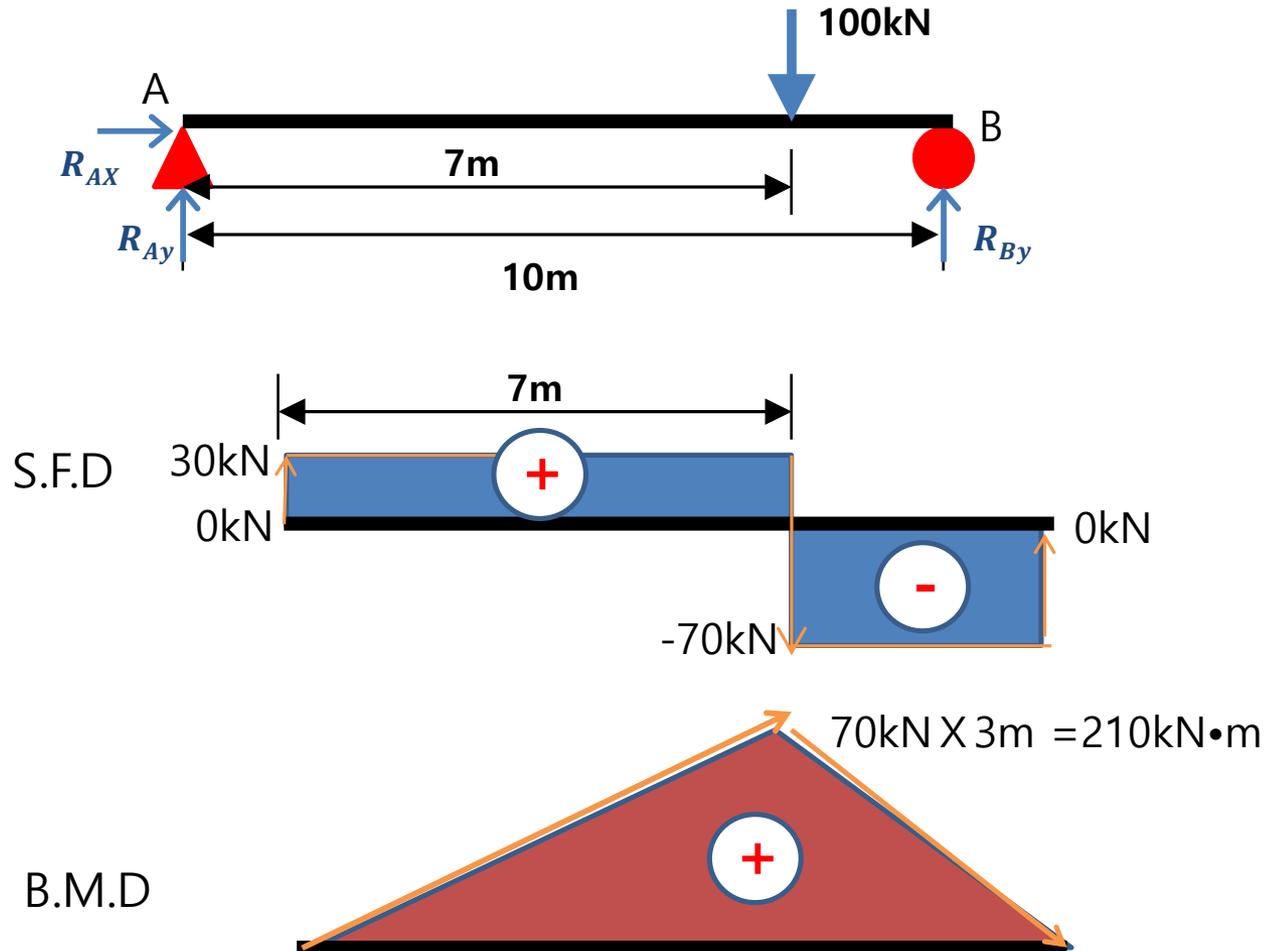
- 구조물 부재 각 단면의 휨모멘트를 나타내는 선도 (예제 2)



# I. 보의 휨응력과 전단응력

## I.3 휨모멘트도 (Bending Moment Diagram : B. M. D)

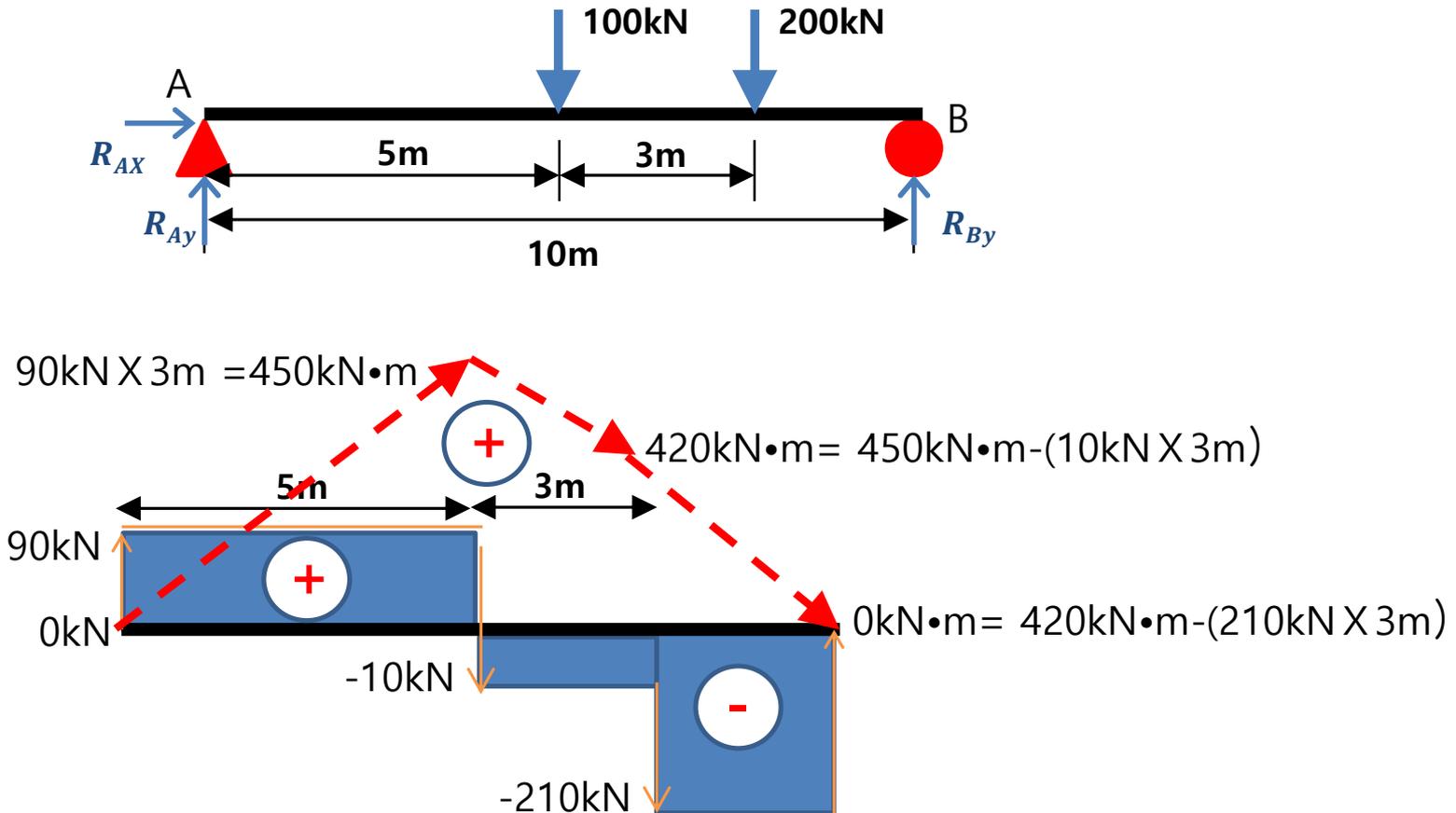
- 구조물 부재 각 단면의 휨모멘트를 나타내는 선도 (예제 3)



# I. 보의 휨응력과 전단응력

## I.3 휨모멘트도 (Bending Moment Diagram : B. M. D)

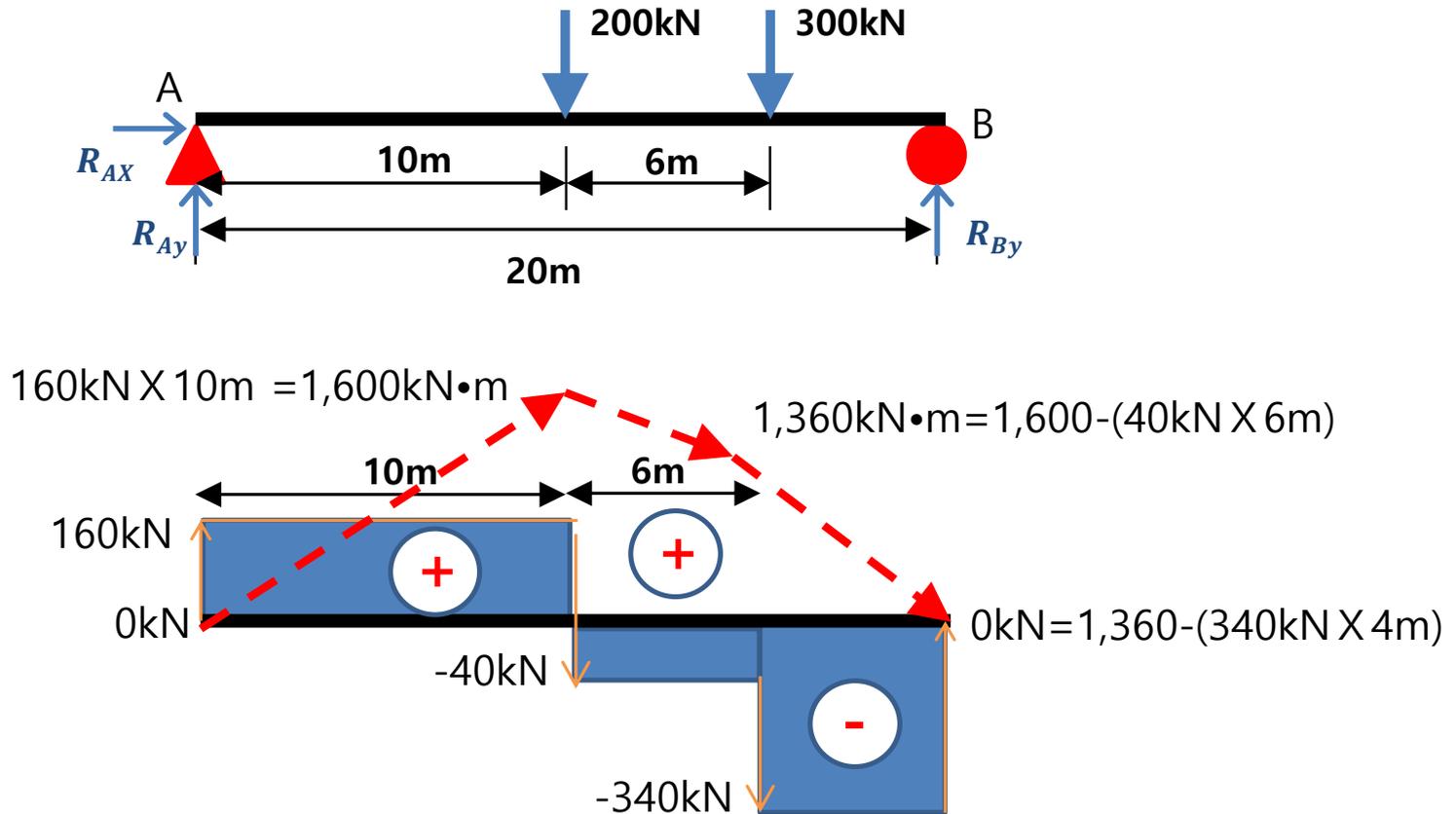
- 구조물 부재 각 단면의 휨모멘트를 나타내는 선도 (예제 4)



# I. 보의 휨응력과 전단응력

## I.3 휨모멘트도 (Bending Moment Diagram : B. M. D)

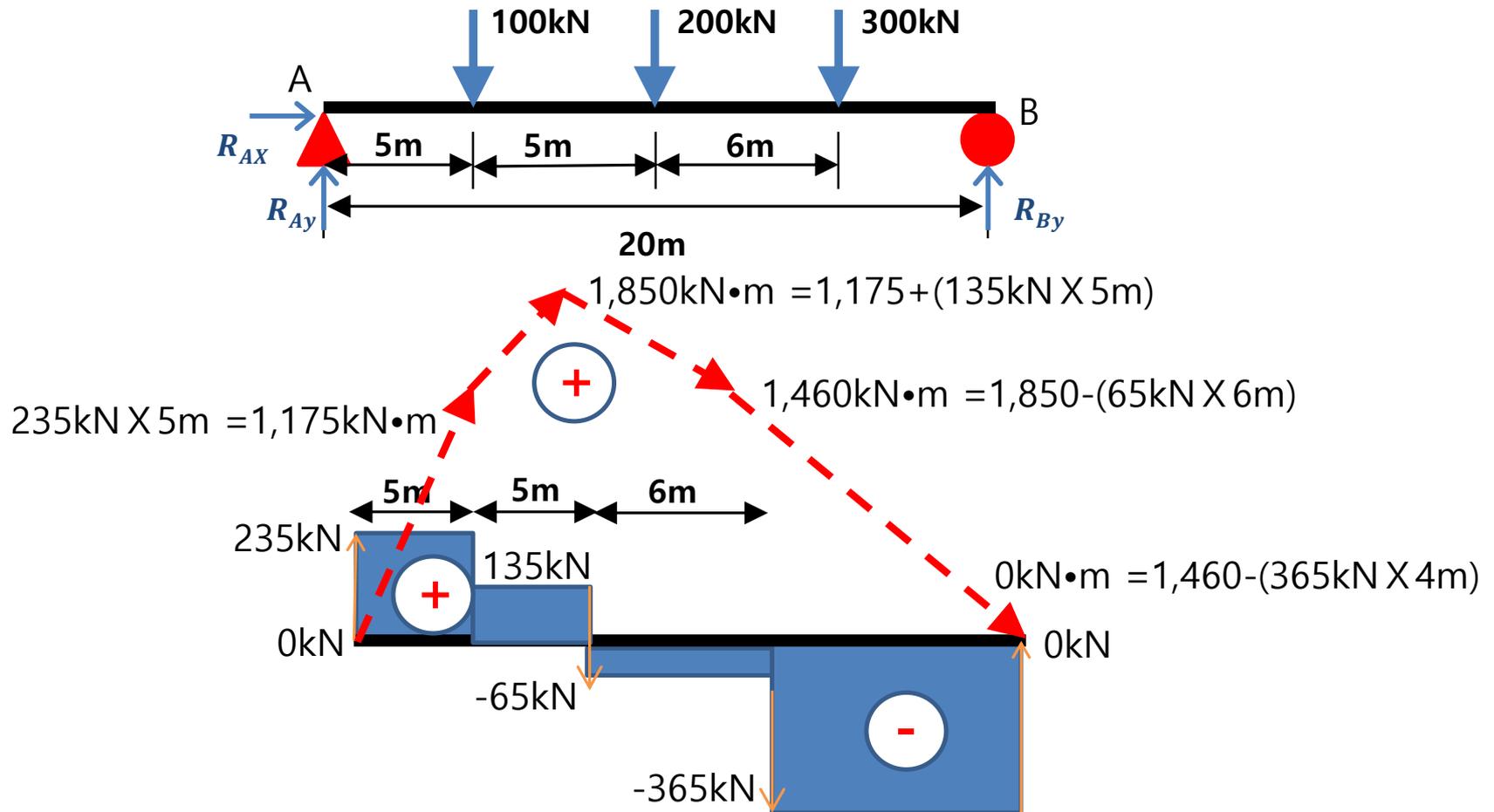
- 구조물 부재 각 단면의 휨모멘트를 나타내는 선도 (예제 5)



# I. 보의 휨응력과 전단응력

## I.3 휨모멘트도 (Bending Moment Diagram : B. M. D)

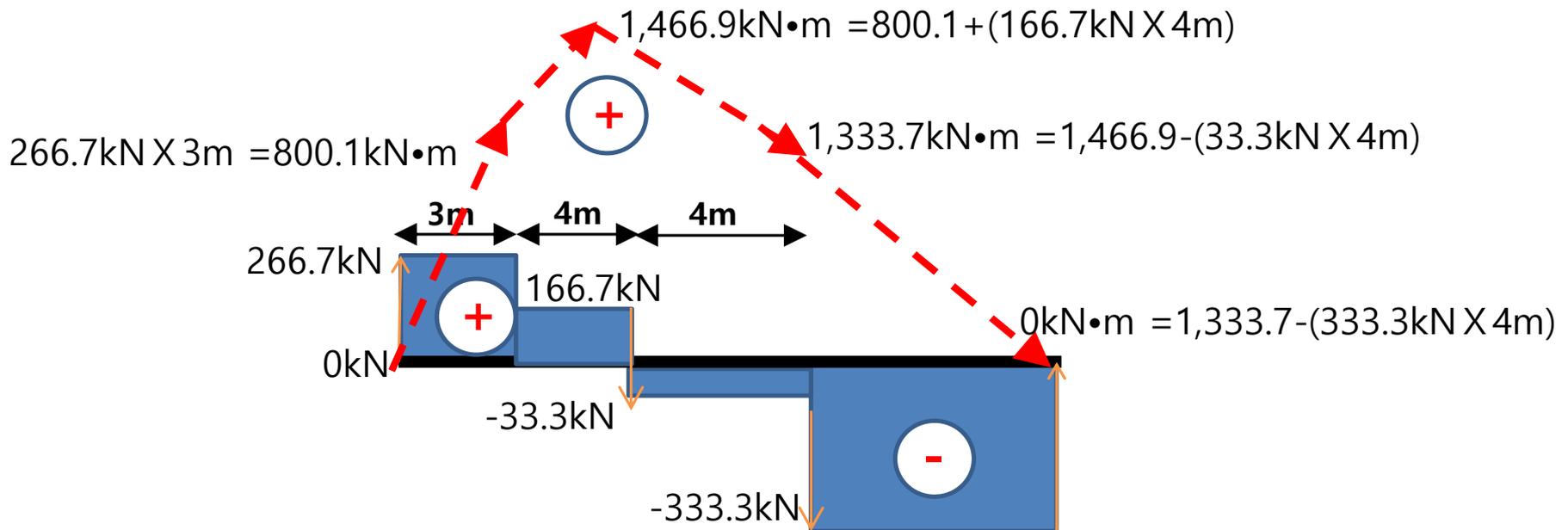
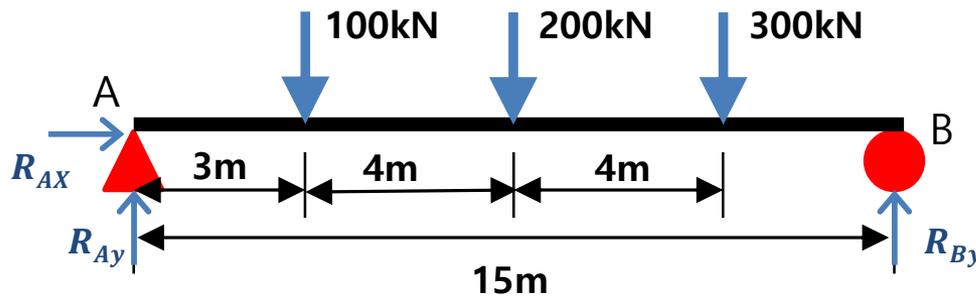
- 구조물 부재 각 단면의 휨모멘트를 나타내는 선도 (예제 6)



# I. 보의 휨응력과 전단응력

## I.3 휨모멘트도 (Bending Moment Diagram : B. M. D)

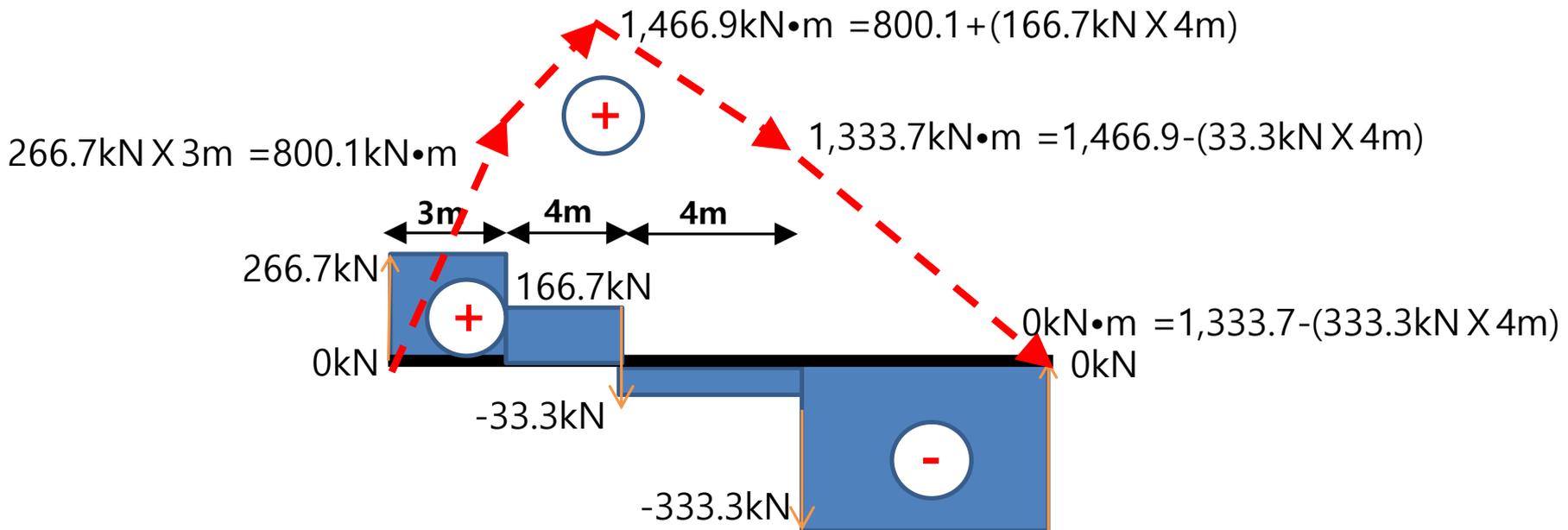
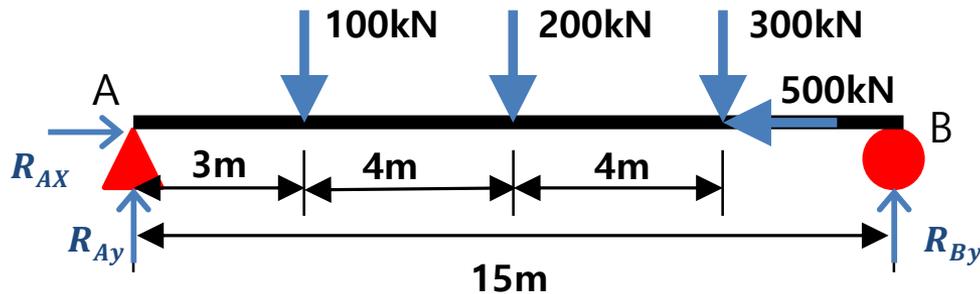
- 구조물 부재 각 단면의 휨모멘트를 나타내는 선도 (예제 7)



# I. 보의 휨응력과 전단응력

## I.3 휨모멘트도 (Bending Moment Diagram : B. M. D)

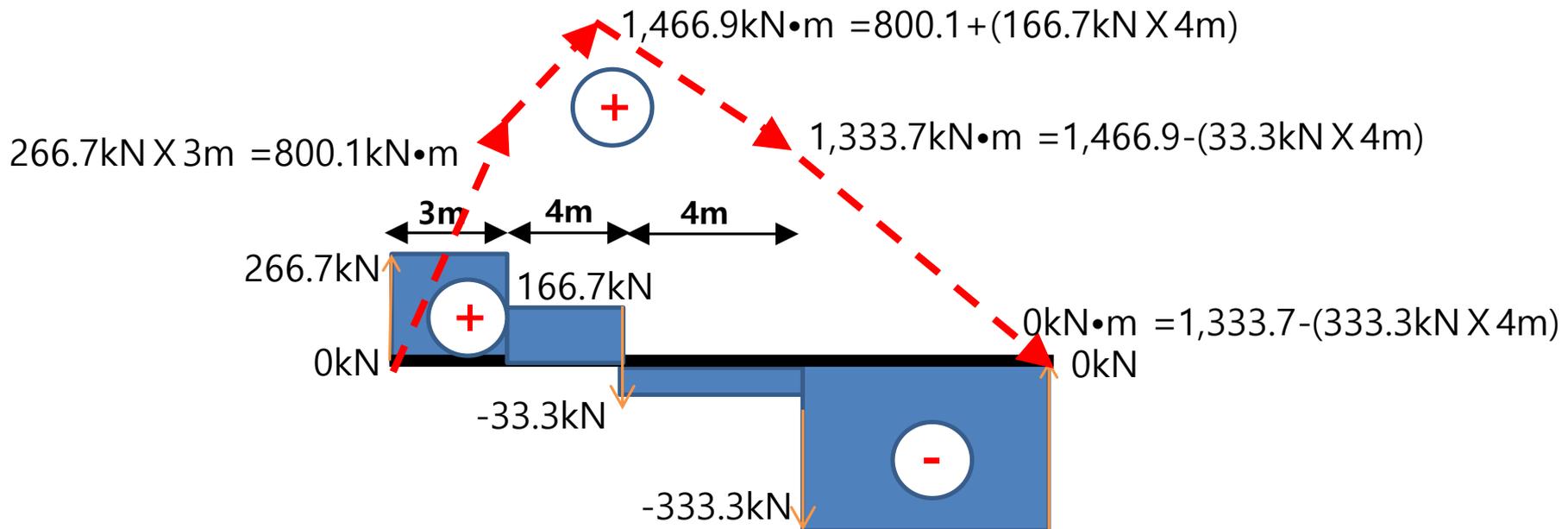
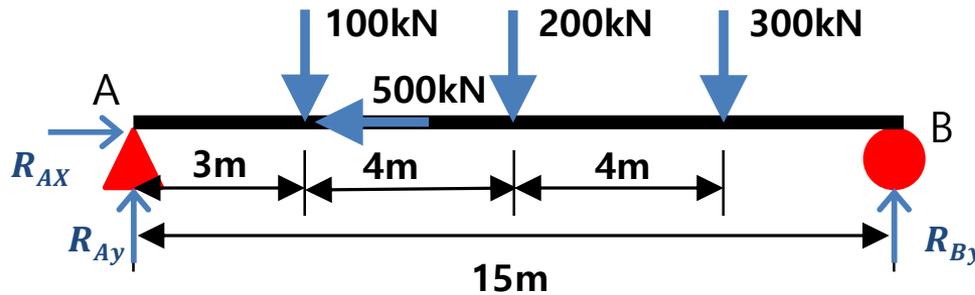
- 구조물 부재 각 단면의 휨모멘트를 나타내는 선도 (예제 8)



# I. 보의 휨응력과 전단응력

## I.3 휨모멘트도 (Bending Moment Diagram : B. M. D)

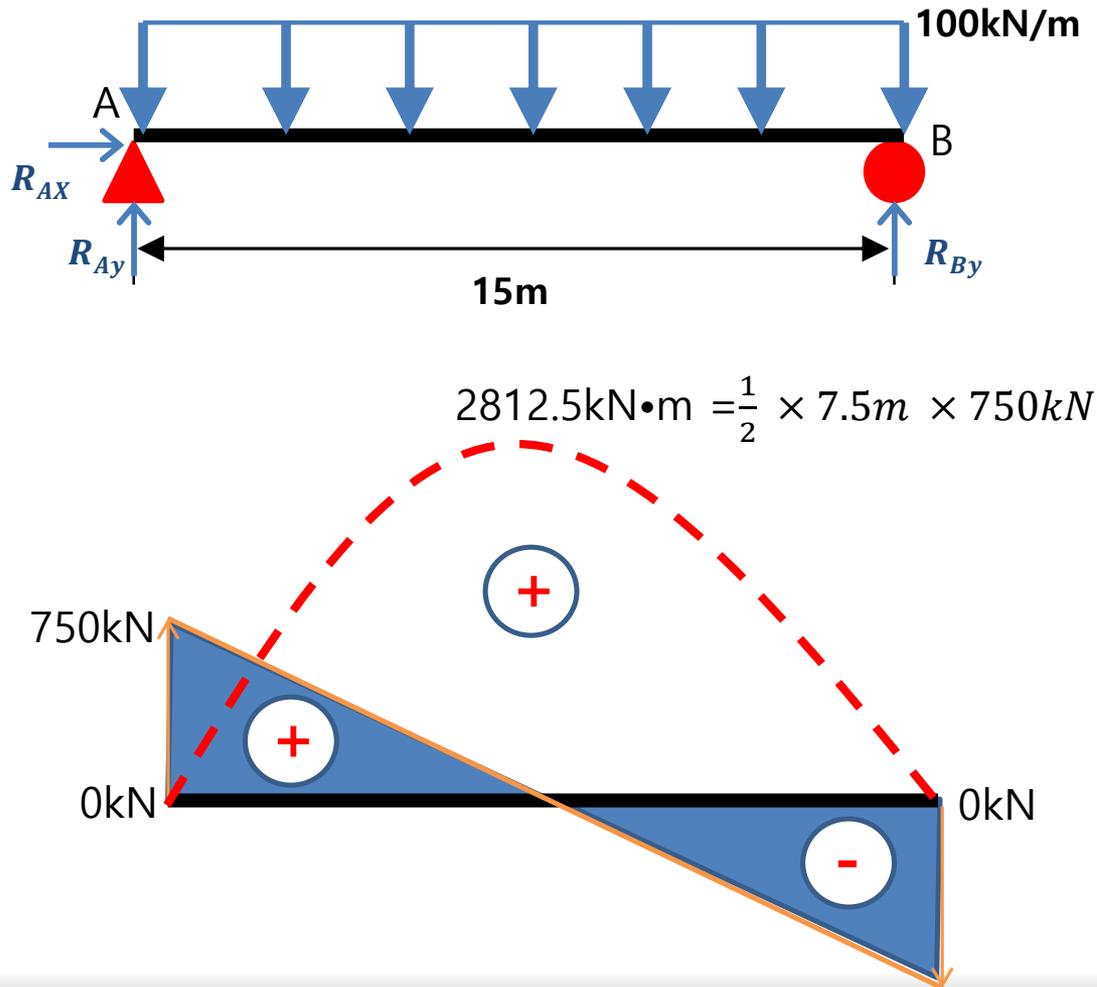
- 구조물 부재 각 단면의 휨모멘트를 나타내는 선도 (예제 9)



# I. 보의 휨응력과 전단응력

## I.3 휨모멘트도 (Bending Moment Diagram : B. M. D)

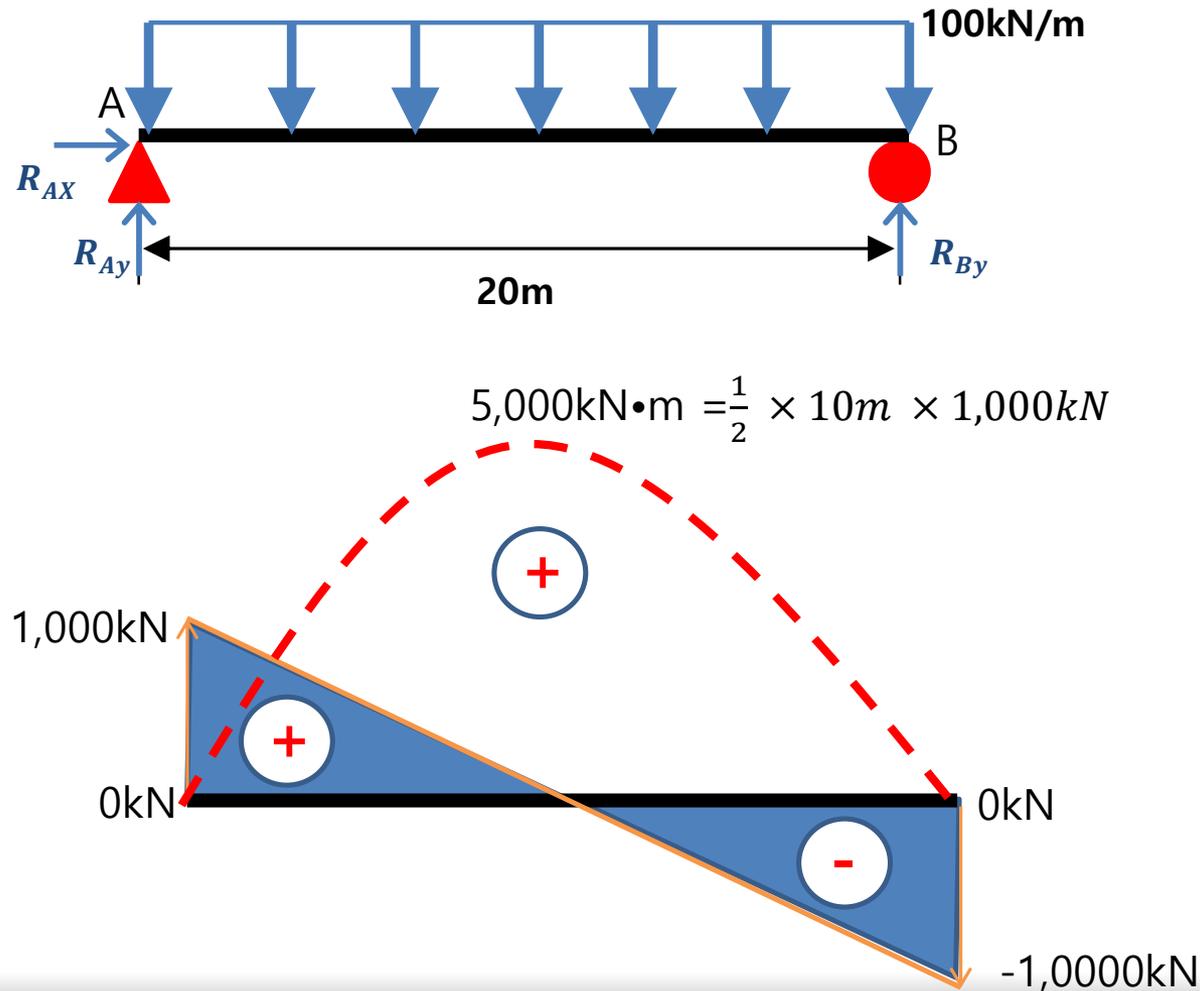
- 구조물 부재 각 단면의 휨모멘트를 나타내는 선도 (예제 10)



# I. 보의 휨응력과 전단응력

## I.3 휨모멘트도 (Bending Moment Diagram : B. M. D)

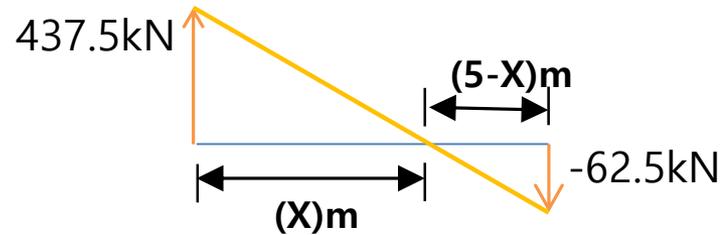
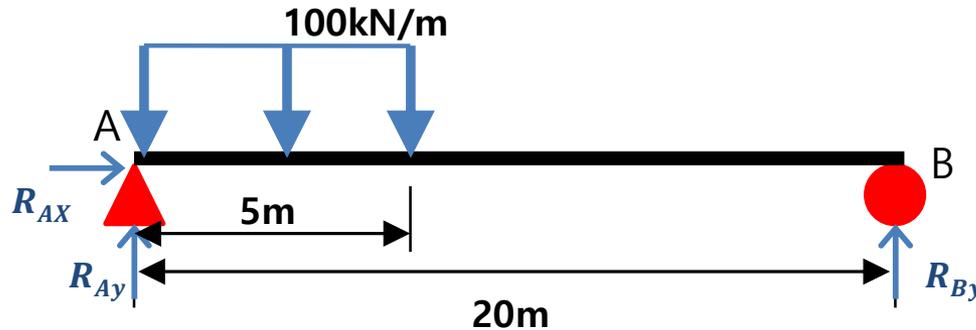
- 구조물 부재 각 단면의 휨모멘트를 나타내는 선도 (예제 11)



# I. 보의 휨응력과 전단응력

## I.3 휨모멘트도 (Bending Moment Diagram : B. M. D)

- 구조물 부재 각 단면의 휨모멘트를 나타내는 선도 (예제 12)



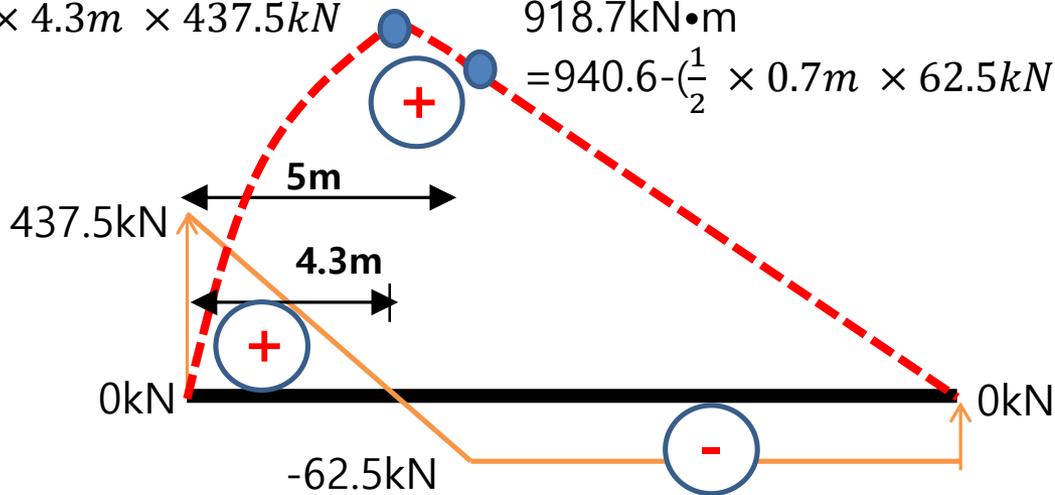
$$940.6\text{kN}\cdot\text{m} = \frac{1}{2} \times 4.3\text{m} \times 437.5\text{kN}$$

$$918.7\text{kN}\cdot\text{m} = 940.6 - \left(\frac{1}{2} \times 0.7\text{m} \times 62.5\text{kN}\right)$$

$$\frac{X}{437.5} = \frac{5-X}{62.5}$$

$$437.5(5-X) = 62.5 X$$

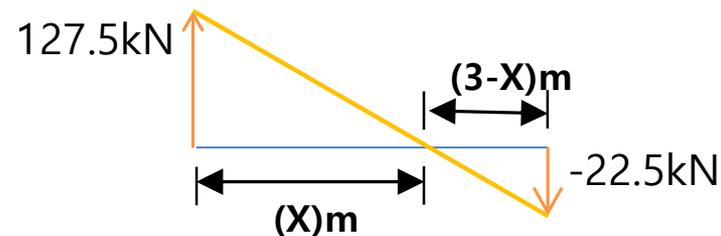
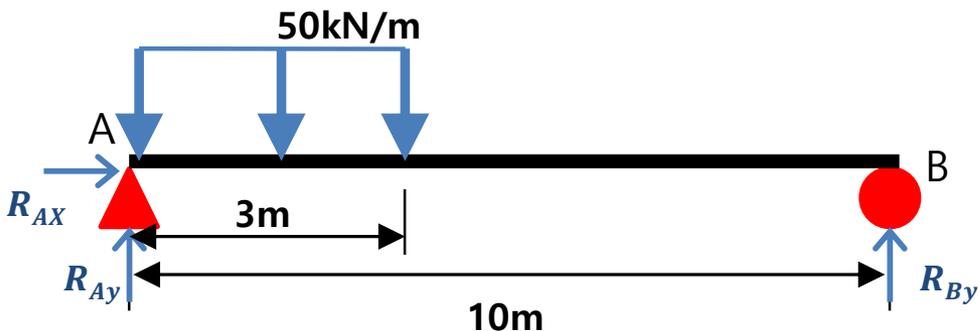
$$500X = 2187.5, X = 4.3\text{m}$$



# I. 보의 휨응력과 전단응력

## I.3 휨모멘트도 (Bending Moment Diagram : B. M. D)

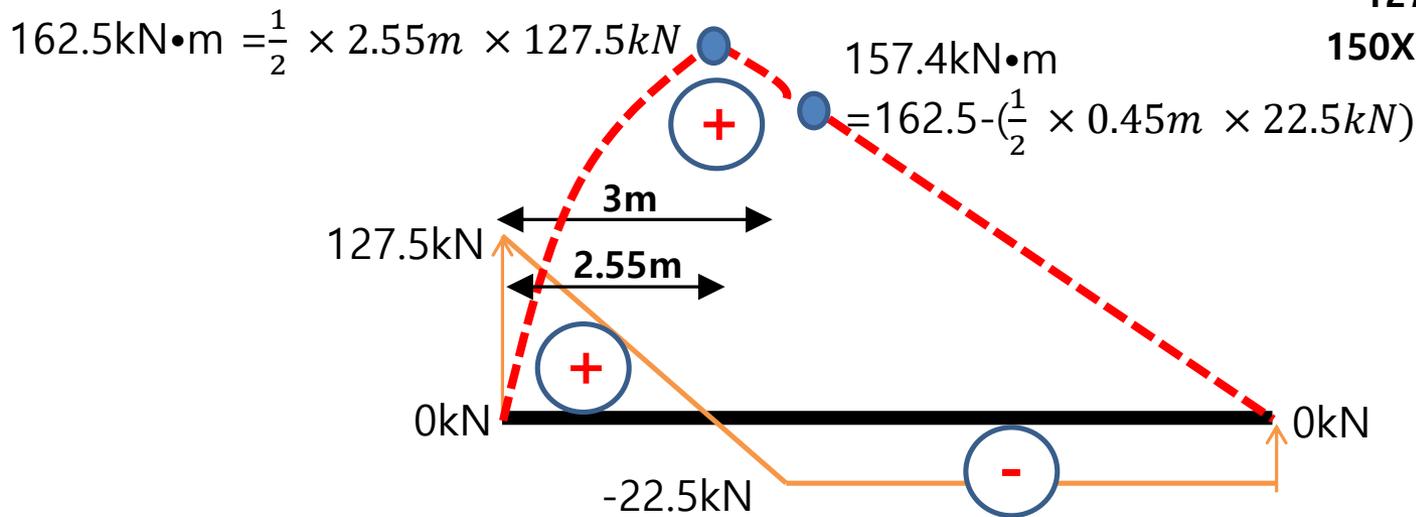
- 구조물 부재 각 단면의 휨모멘트를 나타내는 선도 (예제 13)



$$\frac{X}{127.5} = \frac{3-X}{22.5}$$

$$127.5(3-X) = 22.5 X$$

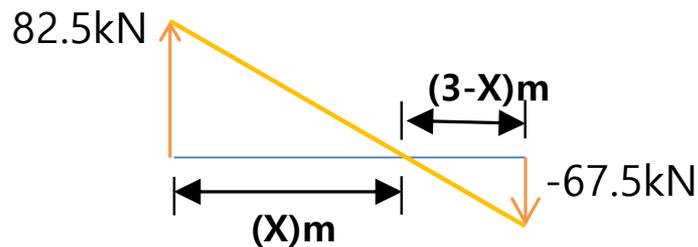
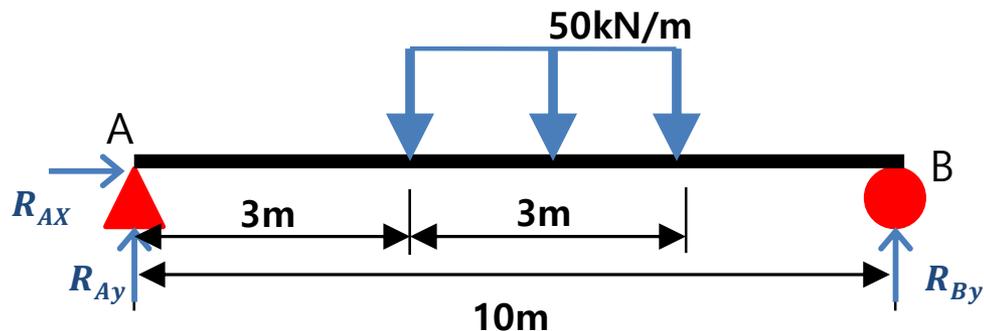
$$150X = 382.5, X = 2.55\text{m}$$



# I. 보의 휨응력과 전단응력

## I.3 휨모멘트도 (Bending Moment Diagram : B. M. D)

- 구조물 부재 각 단면의 휨모멘트를 나타내는 선도 (예제 14)



$$\frac{X}{82.5} = \frac{3-X}{67.5}$$

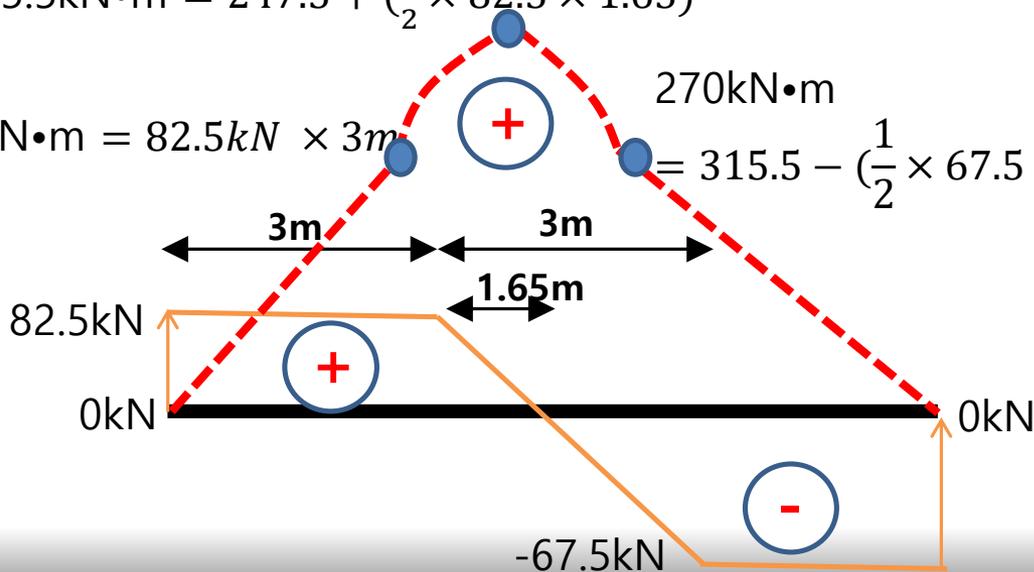
$$82.5(3-X) = 67.5 X$$

$$150X = 247.5, X = 1.65\text{m}$$

$$315.5\text{kN}\cdot\text{m} = 247.5 + \left(\frac{1}{2} \times 82.5 \times 1.65\right)$$

$$247.5\text{kN}\cdot\text{m} = 82.5\text{kN} \times 3\text{m}$$

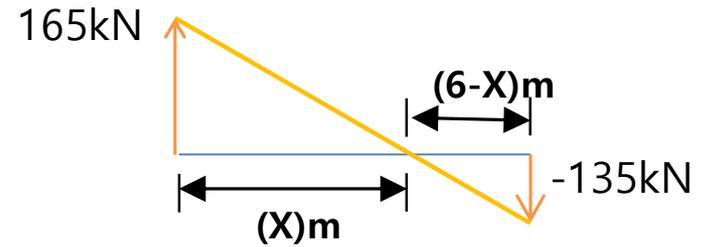
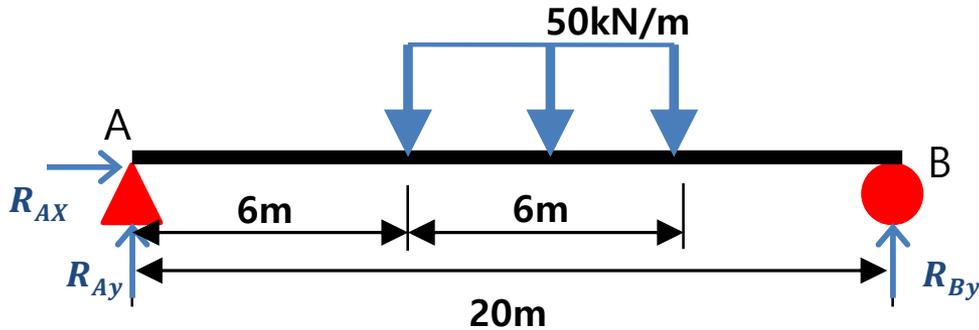
$$= 315.5 - \left(\frac{1}{2} \times 67.5 \times 1.35\right)$$



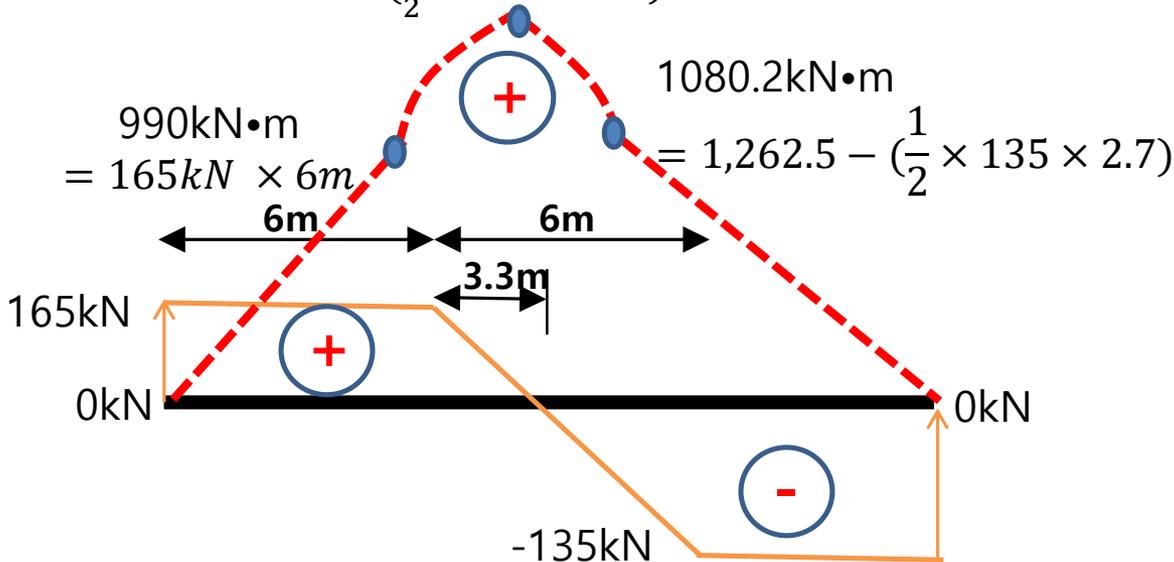
# I. 보의 휨응력과 전단응력

## I.3 휨모멘트도 (Bending Moment Diagram : B. M. D)

- 구조물 부재 각 단면의 휨모멘트를 나타내는 선도 (예제 15)



$$1,262.2\text{kN}\cdot\text{m} = 990 + \left(\frac{1}{2} \times 165 \times 3.3\right)$$



$$\frac{X}{165} = \frac{6 - X}{135}$$

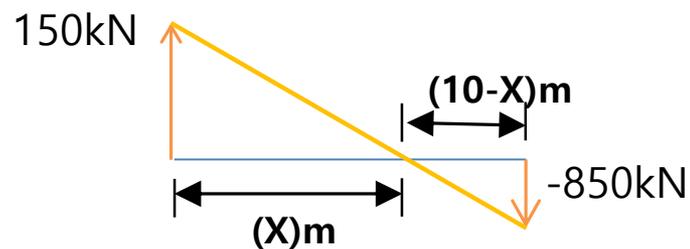
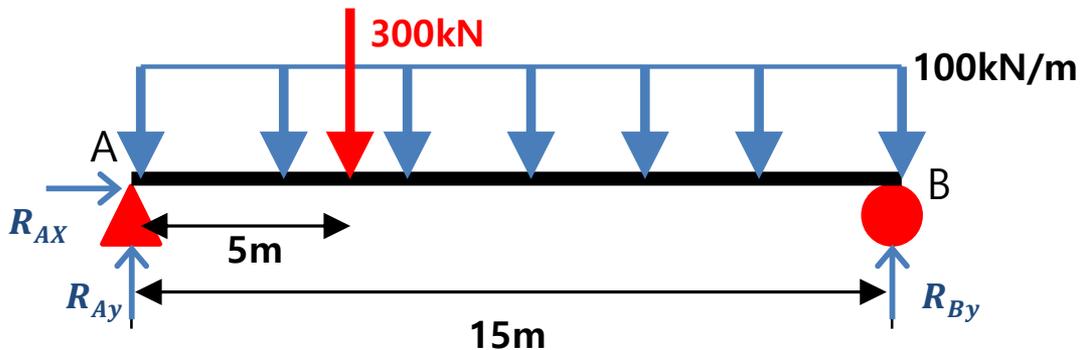
$$165(6 - X) = 135 X$$

$$300X = 990, X = 3.3\text{m}$$

# I. 보의 휨응력과 전단응력

## I.3 휨모멘트도 (Bending Moment Diagram : B. M. D)

- 구조물 부재 각 단면의 휨모멘트를 나타내는 선도 (예제 16)



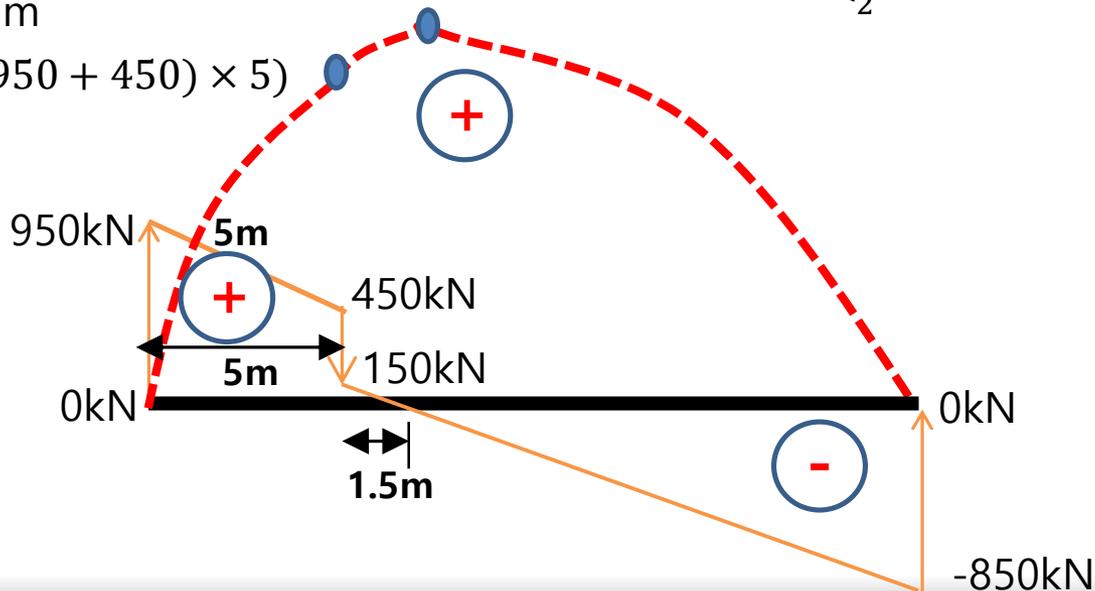
$$3,500 \text{ kN}\cdot\text{m} = \left(\frac{1}{2} \times (950 + 450) \times 5\right)$$

$$3,612.5 \text{ kN}\cdot\text{m} = 3,500 + \left(\frac{1}{2} \times 150 \times 1.5\right)$$

$$\frac{X}{150} = \frac{10 - X}{850}$$

$$150(10 - X) = 850X$$

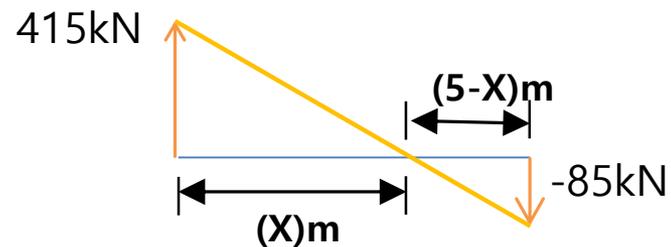
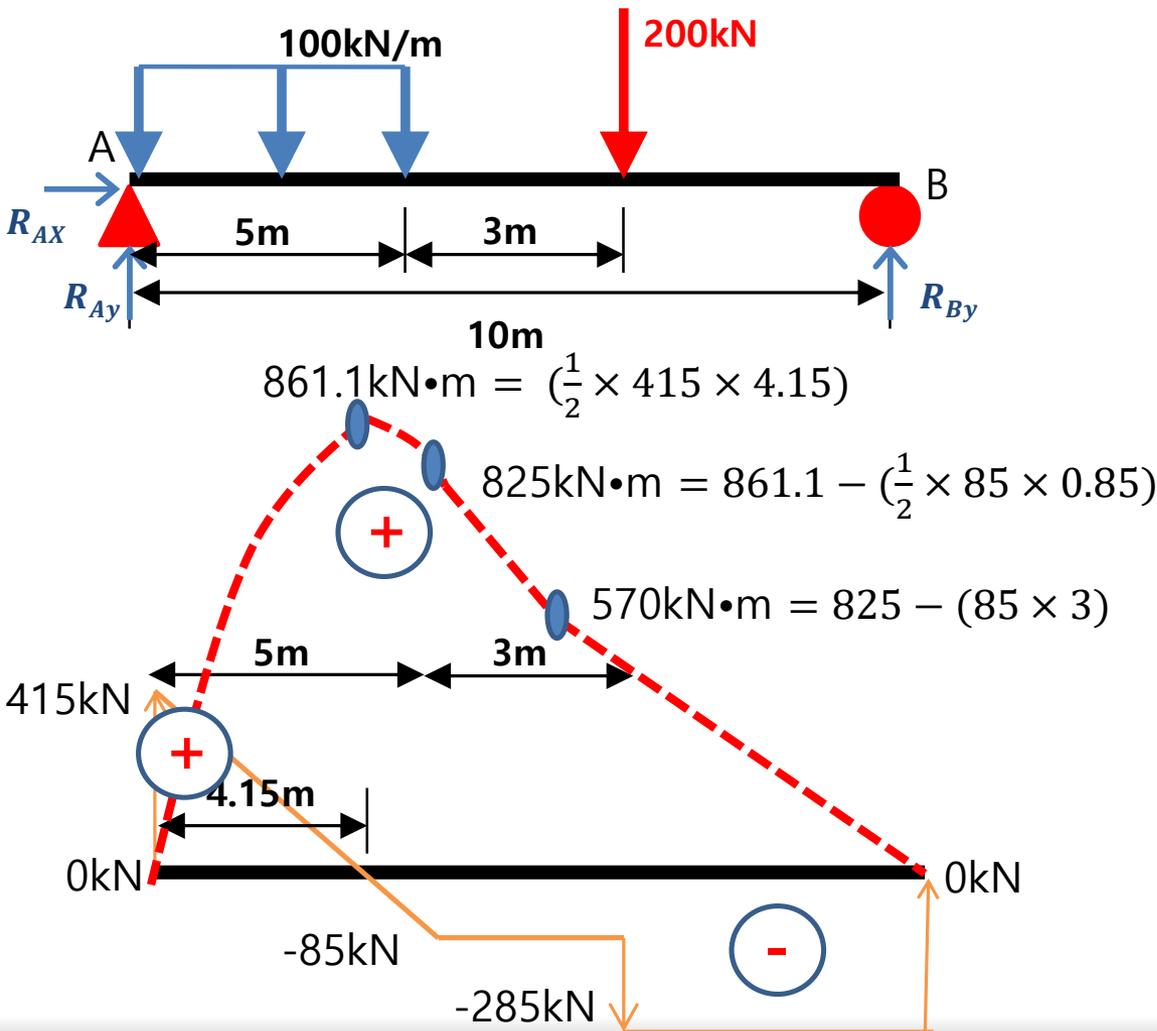
$$1,000X = 1,500, X = 1.5 \text{ m}$$



# I. 보의 휨응력과 전단응력

## I.3 휨모멘트도 (Bending Moment Diagram : B. M. D)

- 구조물 부재 각 단면의 휨모멘트를 나타내는 선도 (예제 17)



$$\frac{X}{415} = \frac{5-X}{85}$$

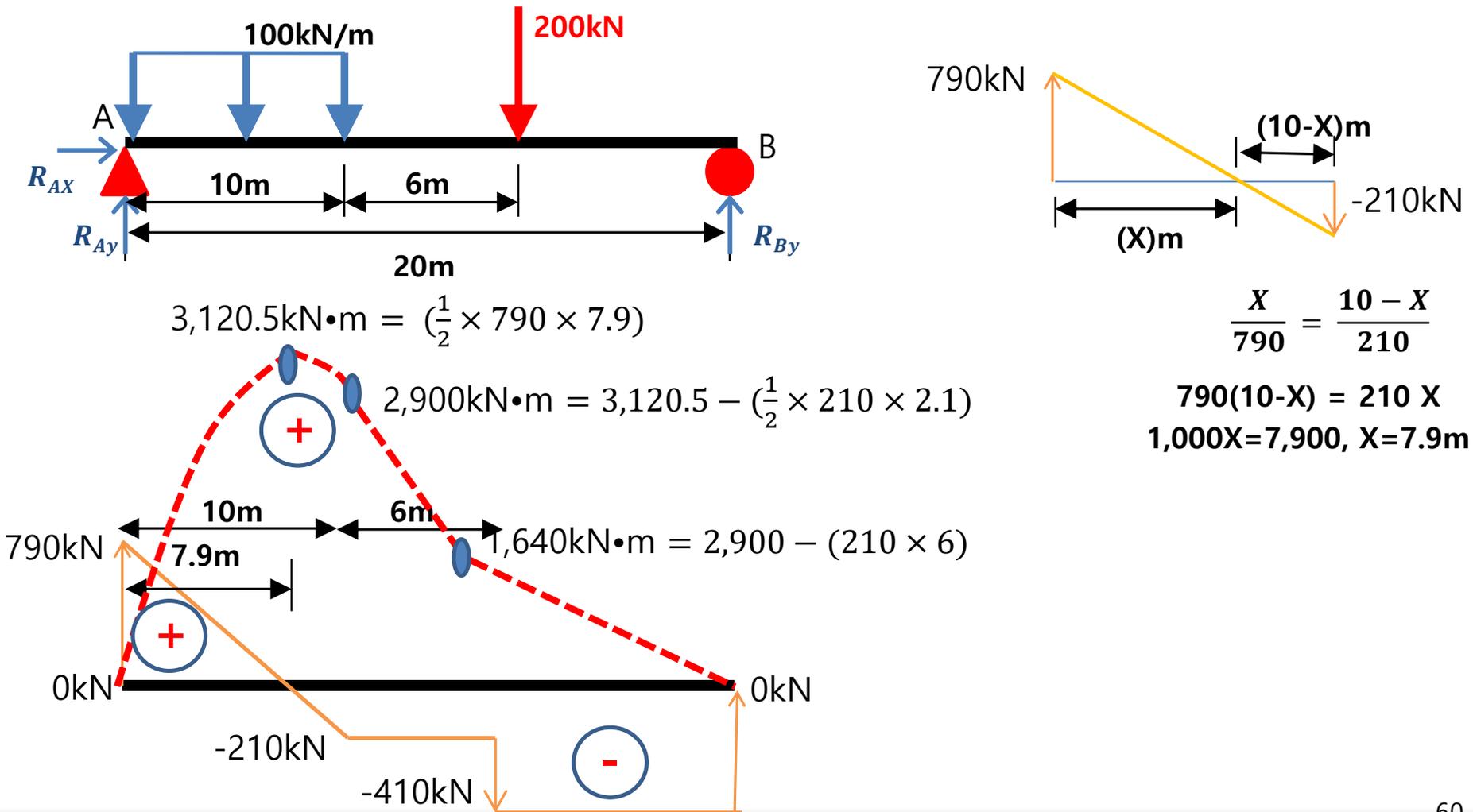
$$415(5-X) = 85X$$

$$500X = 2,075, X = 4.15\text{m}$$

# I. 보의 휨응력과 전단응력

## I.3 휨모멘트도 (Bending Moment Diagram : B. M. D)

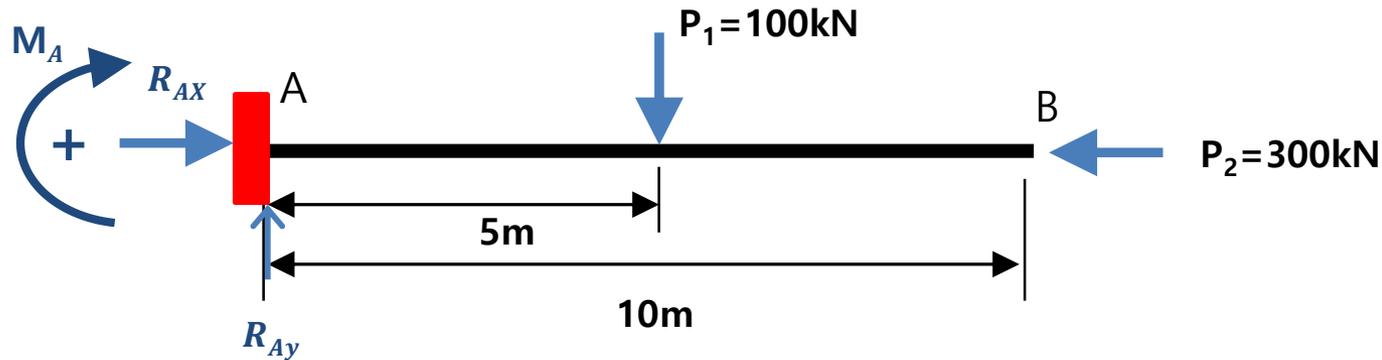
- 구조물 부재 각 단면의 휨모멘트를 나타내는 선도 (예제 18)



# I. 보의 휨응력과 전단응력

## I.3 휨모멘트도 (Bending Moment Diagram : B. M. D)

- 구조물 부재 각 단면의 휨모멘트를 나타내는 선도 (예제 22)



$$M_A + \curvearrowright = 0, \quad M_A + (100\text{kN} \times 5\text{m}) = 0, \quad M_A = -500\text{kN}\cdot\text{m}$$

